

UNIVERSITY OF ILLINOIS  
AT URBANA-CHAMPAIGN

# Phonon Scattering and Thermal Conduction in Nanostructured Semiconductors

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# Outline

- Distribution of phonon mean-free-paths and nanostructure effects on thermal conductivity.
- Thermal conductivity of nanostructured materials
  - GaN/AlN and oxide superlattices
  - PbSe/PbTe nanodot superlattices
  - rough Si nanowires
- Bottom line: not difficult for nanostructuring to make bad thermoelectrics into mediocre thermoelectrics, but difficult to significantly improve good thermoelectrics

# Reduce lattice thermal conductivity without (significantly) reducing charge-carrier mobility

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## Nanostructured Thermoelectrics: Big Efficiency Gains from Small Features

By *Christopher J. Vineis, Ali Shakouri, Arun Majumdar, and Mercouri G. Kanatzidis\**

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## Thermoelectric Nanostructures: From Physical Model Systems towards Nanograined Composites

*Kornelius Nielsch,\* Julien Bachmann, Johannes Kimling, and Harald Böttner*

[www.afm-journal.de](http://www.afm-journal.de)

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## Nanostructured Bulk Silicon as an Effective Thermoelectric Material

By *Sabah K. Bux, Richard G. Blair, Pawan K. Gogna, Hohyun Lee, Gang Chen, Mildred S. Dresselhaus, Richard B. Kaner, and Jean-Pierre Fleurial\**

# Heat is carried by phonons with a broad distribution of mean-free-paths

- Thermal conductivity is an integral property: difficult to understand and control.
- Simplest case of thermal conductivity where resistive scattering dominates.

$$\Lambda = \frac{1}{3} \int_0^{\omega_c} c(\omega) v_g^2(\omega) \tau(\omega) d\omega$$

$c(\omega)$  = heat capacity of phonon mode

$v_g(\omega)$  = phonon group velocity

$\tau(\omega)$  = scattering time

$\omega_c$  = cut-off frequency

## Make a “Klemens-like” calculation

- Assume linear dispersion for  $\omega < \omega_c$  and  $\tau^{-1} \propto \omega^2 T$

$$\Lambda = \frac{A}{T} \int_0^{\omega_c} d\omega = \frac{A}{T} \omega_c$$

- Convert to an integral over mean-free-path  $l = \frac{B}{\omega^2 T}$

$$\Lambda = \frac{A\sqrt{B}}{2T^{3/2}} \int_{l_c}^{\infty} \frac{1}{l^{3/2}} dl$$

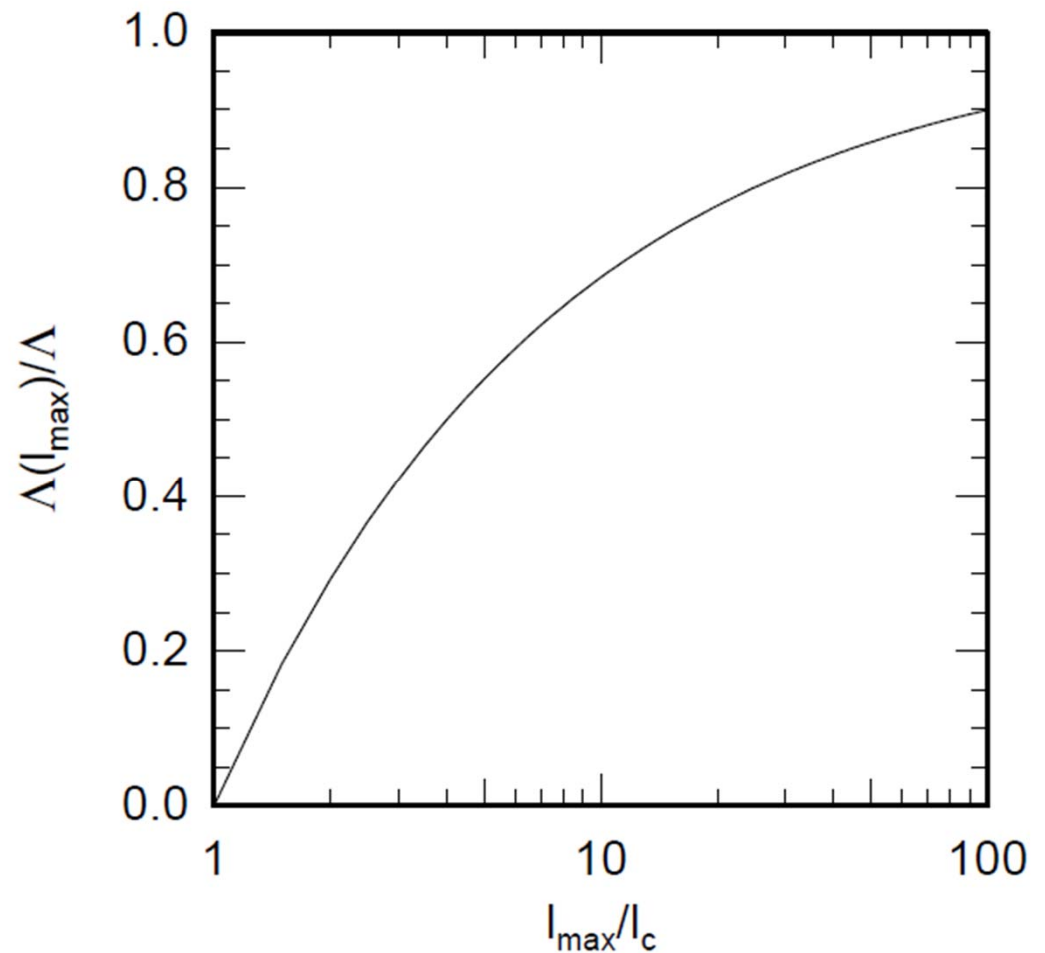
$$\frac{\Lambda(l_{\max})}{\Lambda} = 1 - \left( \frac{l_c}{l_{\max}} \right)^{1/2}$$

$l_c$  is the mean-free-path at the cut-off frequency

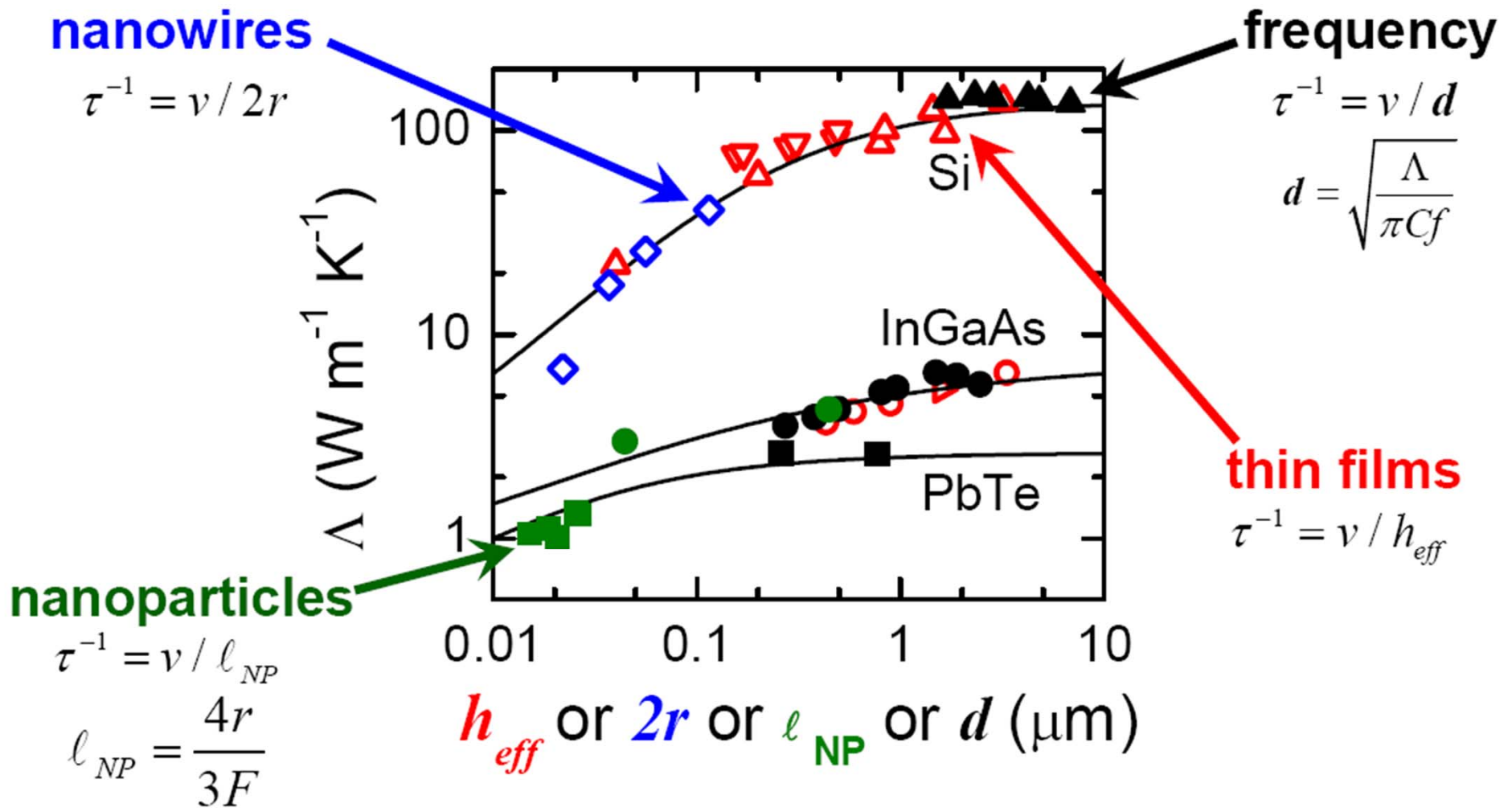
$l_{\max}$  is the maximum mean-free-path that contributes to  $\Lambda$

# Heat is carried by phonons with a broad distribution of mean-free-paths

- Phonon scattering by charge carriers or boundaries will narrow the distribution.
- Alloying and point defects will broaden the distribution.
- Relaxational damping will eventually be a limiting factor.
- Details are probably important (scattering rates, normal processes, dispersion...)



# Summary of nanostructure effects

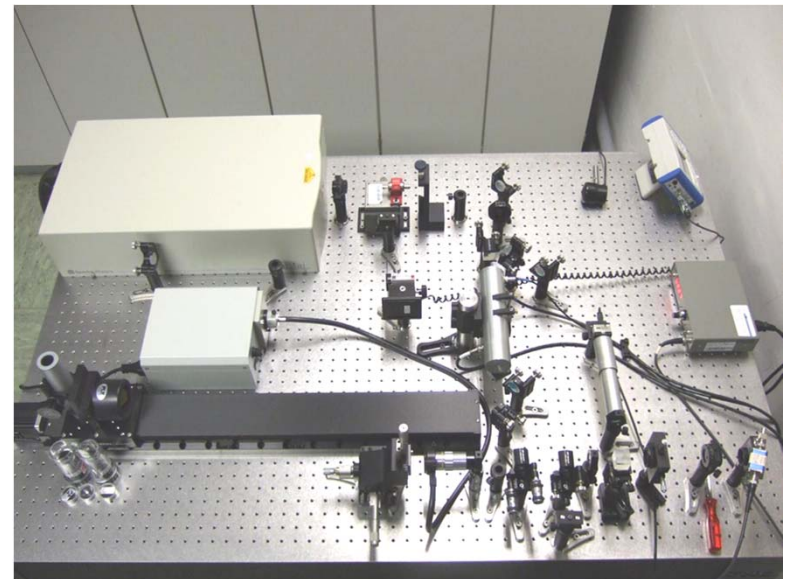
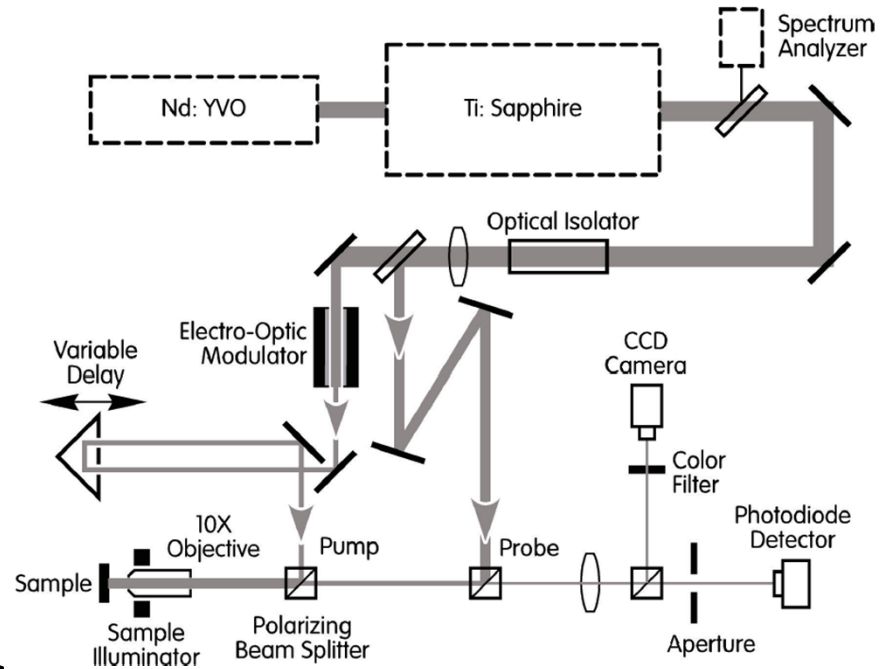


$F$ =volume fraction,  $r$ =radius

Yee Kan Koh, unpublished

# Time domain thermoreflectance since 2003

- Improved optical design
- Normalization by out-of-phase signal eliminates artifacts, increases dynamic range and improves sensitivity
- Exact analytical model for Gaussian beams and arbitrary layered geometries
- One-laser/two-color approach tolerates diffuse scattering

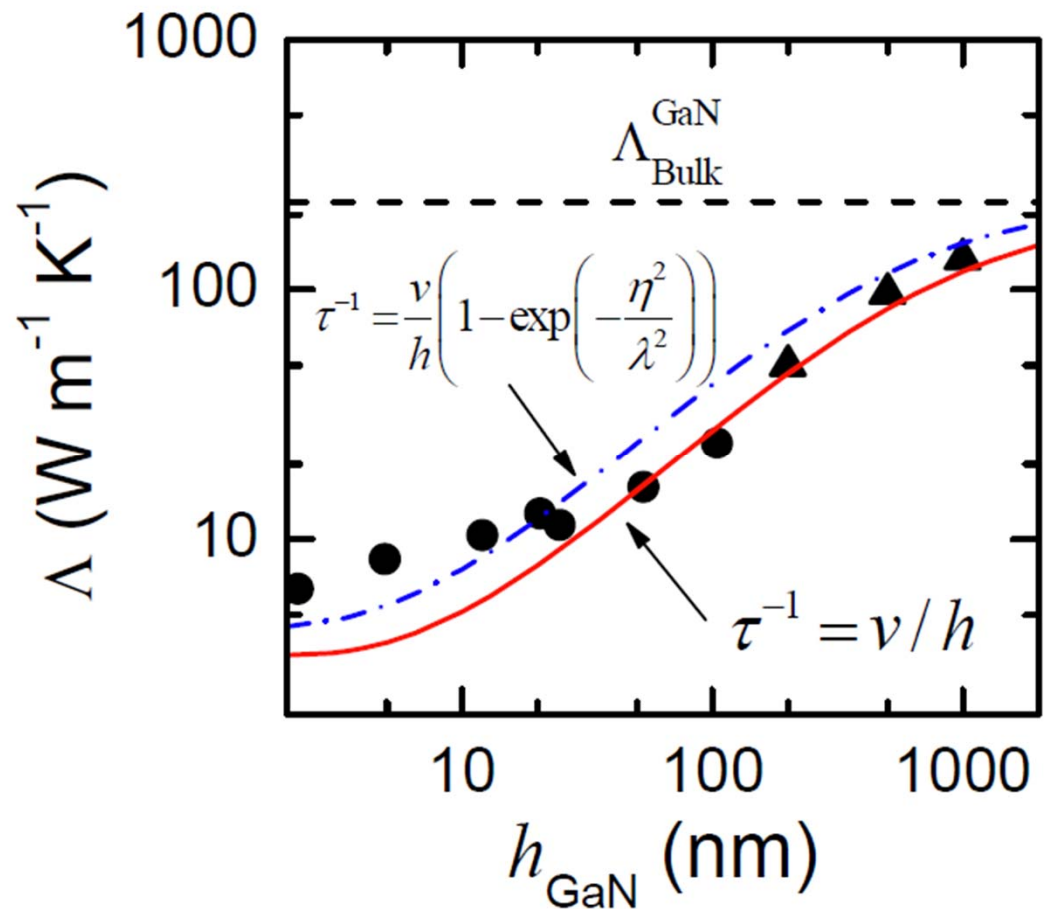


Clone built at Fraunhofer Institute for Physical Measurement, Jan. 7-8 2008



# AlN/GaN superlattices

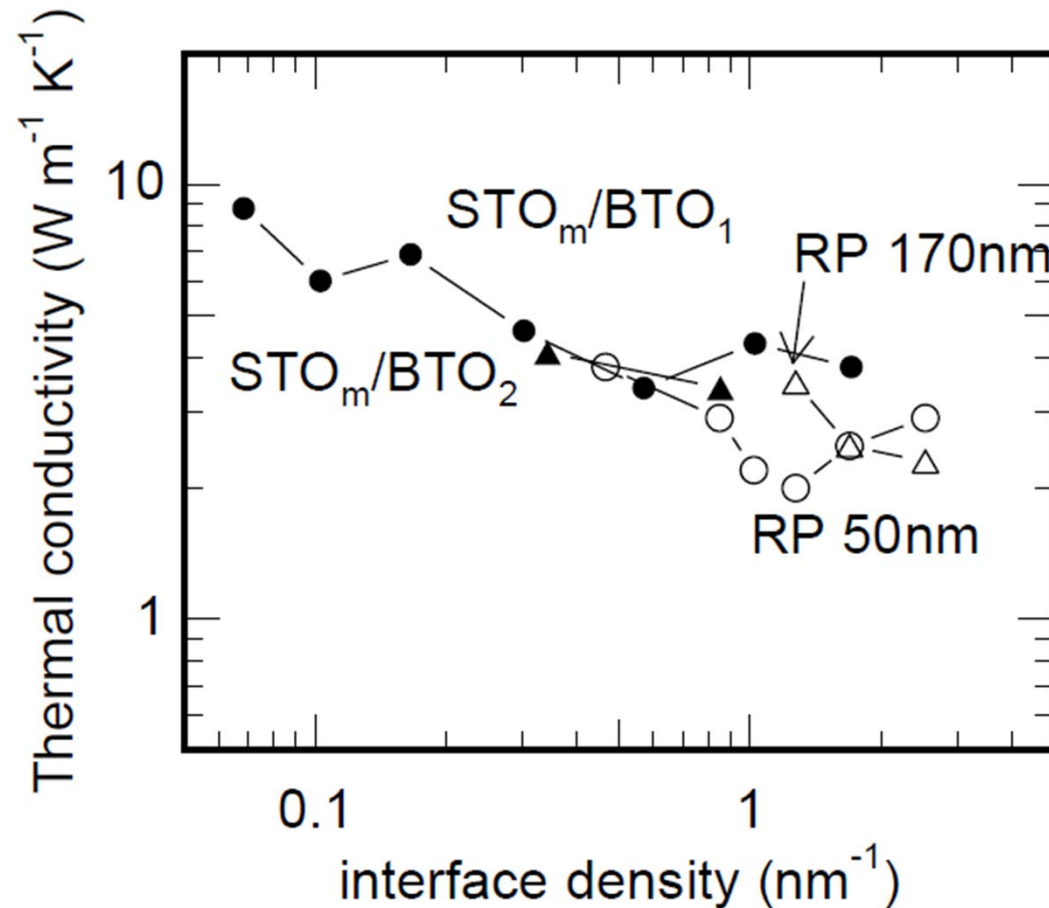
- Strained AlN 4 nm
- Vary GaN thickness  $2 < h_{\text{GaN}} < 1000$  nm
- Data suggest that long wave-length end of phonon distribution is not diffusively scattered
- No evidence of coherent phonon scattering (e.g., minimum created by reduction in group velocity)



Collaboration with D. Jena, Koh *et al.*, Adv. Funct. Mater. (2009)

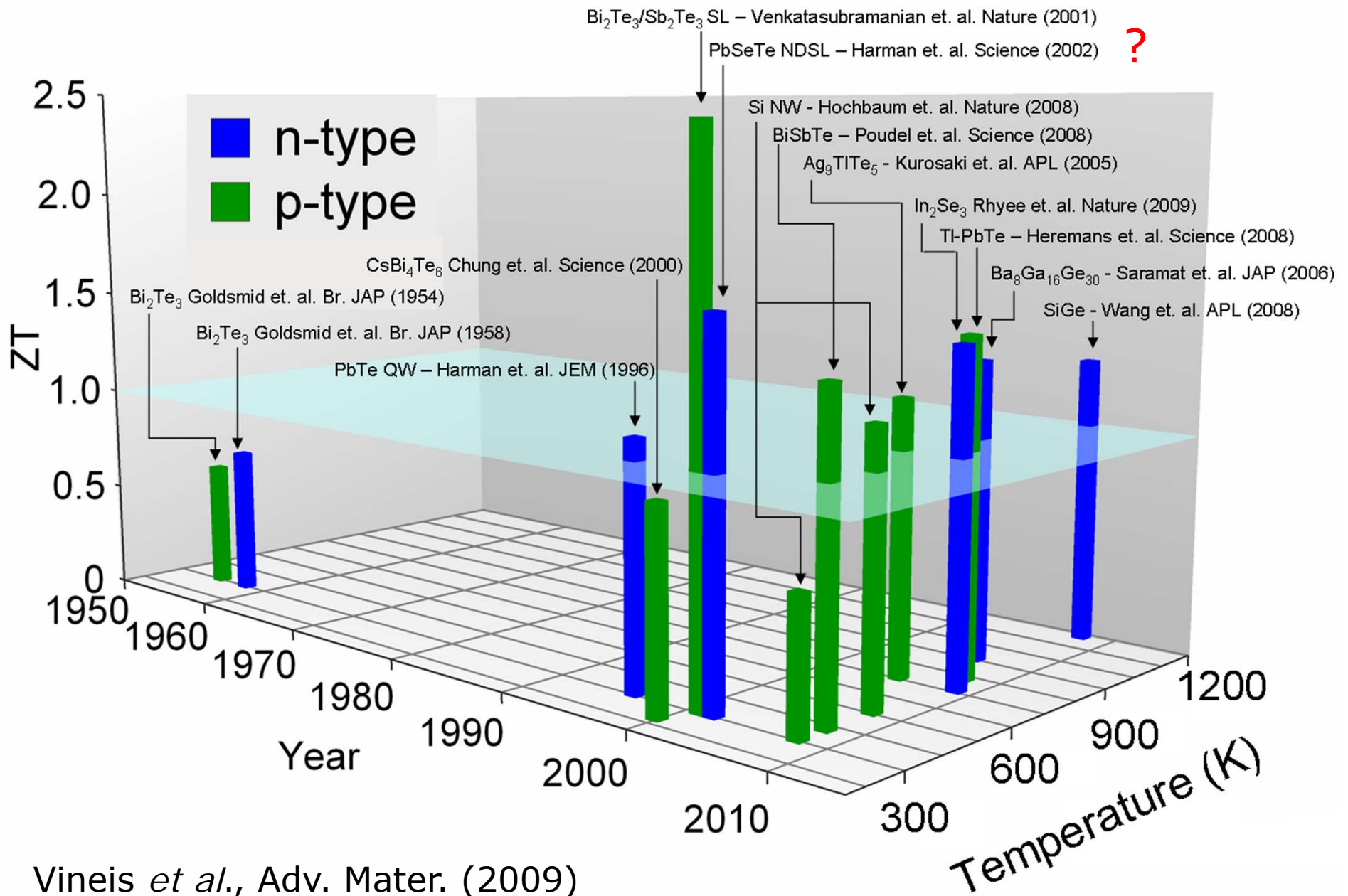
# Work in progress: short period perovskite superlattices and RP phases.

- No evidence (yet) of coherent phonon scattering (e.g., minimum created by reduction in group velocity)



Collaboration with Mark Zurbuchen (UCLA) and D. Schlom's group (Cornell)

# Progress in increasing figure of merit ZT



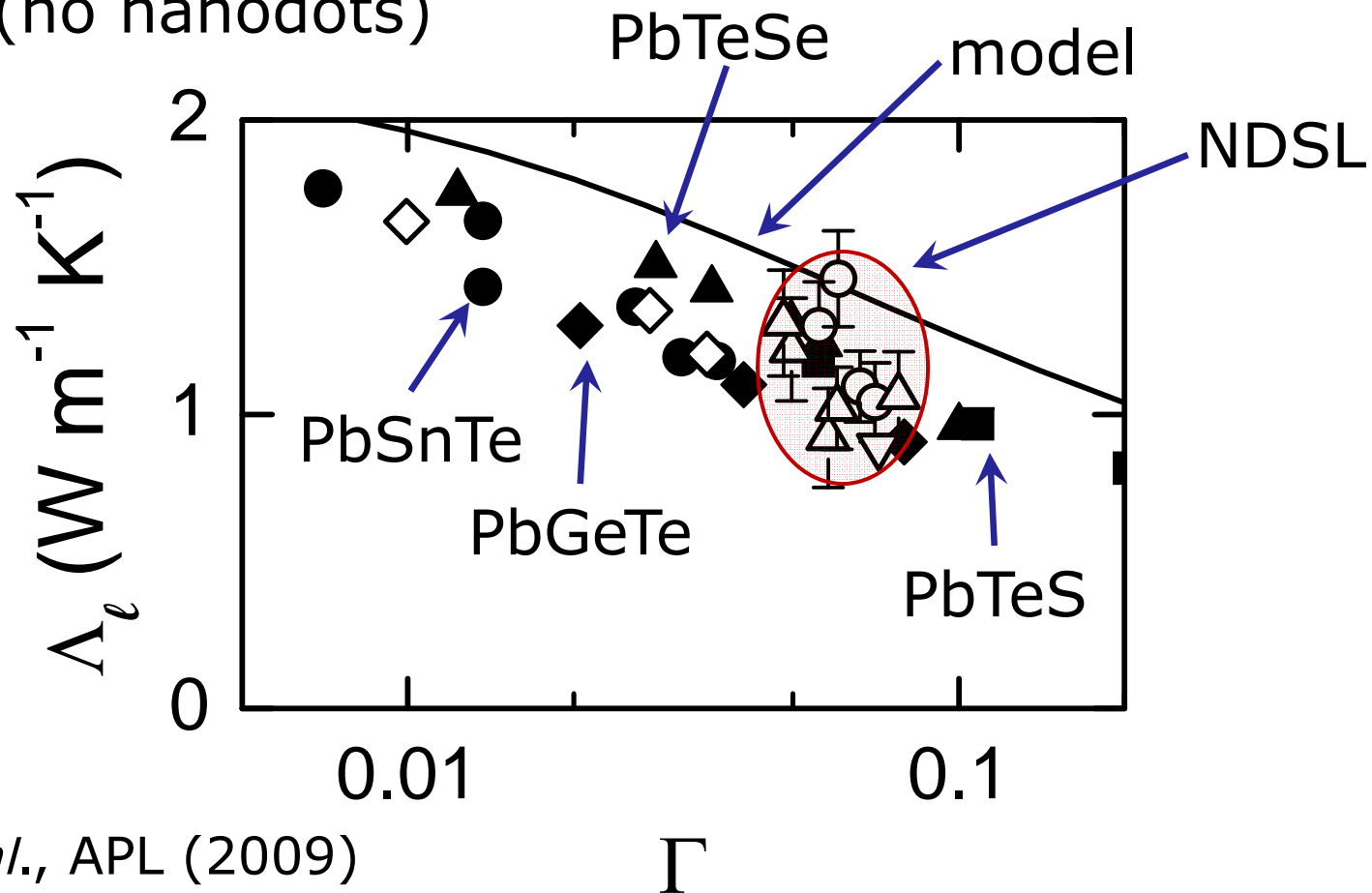
Vineis *et al.*, Adv. Mater. (2009)

## ZT=1.6 reported for PbTe/PbSe nanodot superlattices (NDSL) thermoelectric materials

- Power factor is not enhanced so lattice thermal conductivity is assumed to be very small
- Limited data for thermal conductivity
- Use TDTR to measure the total thermal conductivity in the **top  $\sim 0.5\text{-}\mu\text{m}$**  of a large number of  **$\sim 5\text{-}\mu\text{m}$ -thick** NDSL samples grown at MIT/Lincoln-Lab
- In-plane electrical measurements (conductivity, Hall) give estimate of electrical thermal conductivity,  $\Lambda_{lat} = \Lambda_{total} - \Lambda_{elec}$
- Assume that anisotropy is “not too strong”

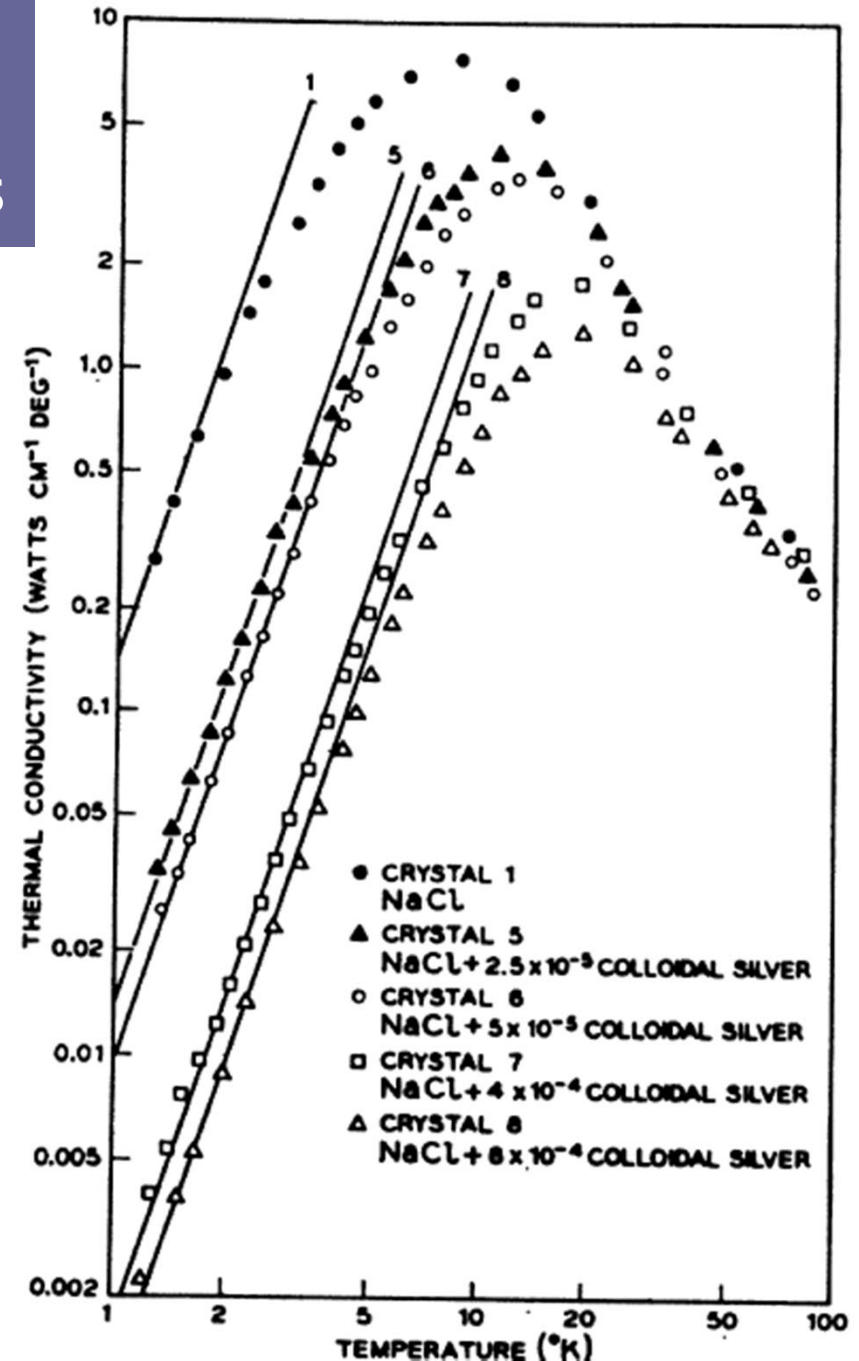
# NDSL and superlattice PbTe do not significantly beat the alloy limit

- nanostructured (open symbols); random alloys (filled symbols);
- Rayleigh scattering strength  $\Gamma$  calculated for random alloy (no nanodots)



Need high densities of precipitates to make a difference at high temperatures

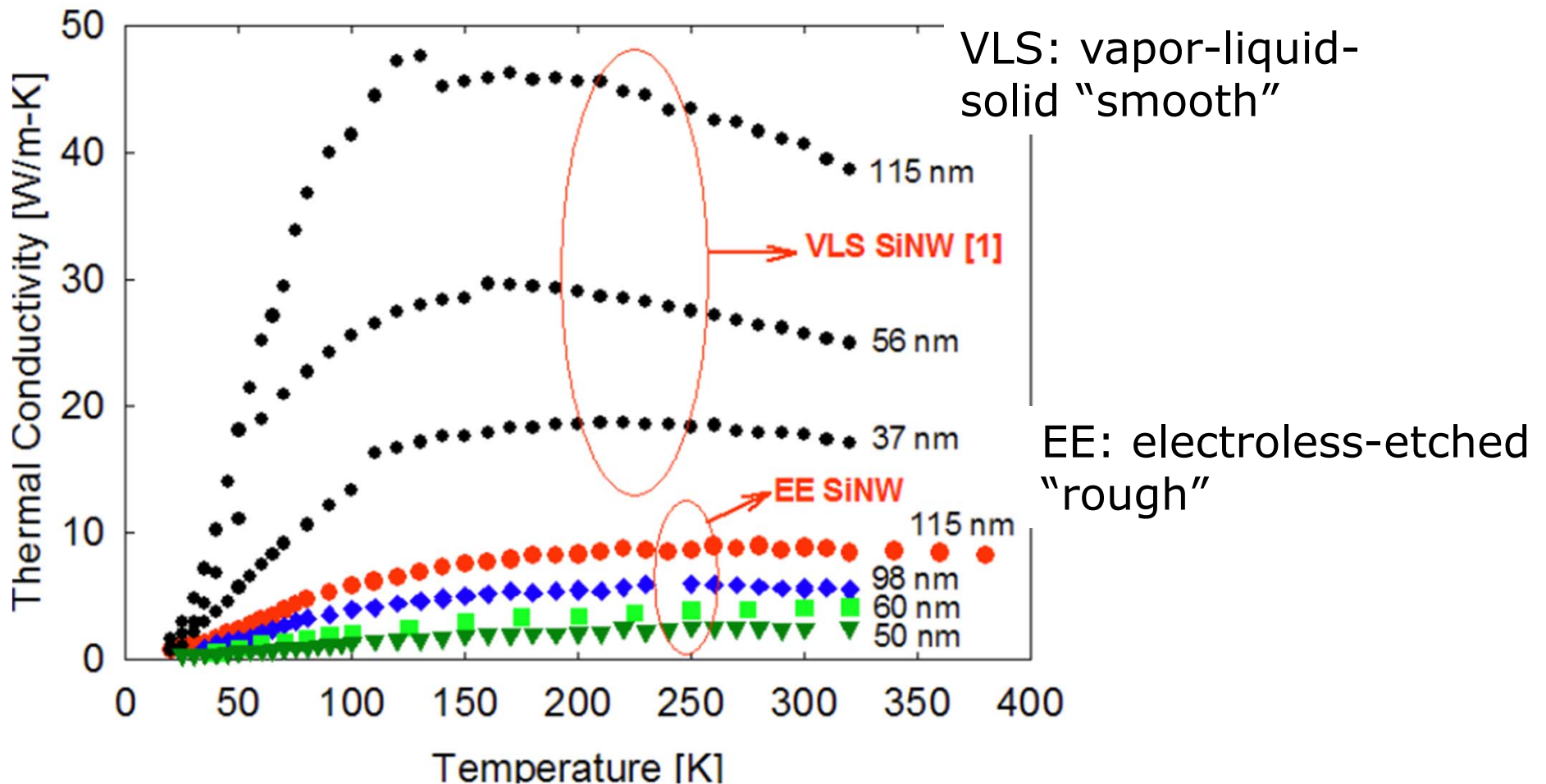
- Reduction of NaCl:AgCl mixed crystal in K vapor at 600 °C.
- Ag particle radii  $r \approx 15$  nm
- Mean-free-path is  $\ell = 40$   $\mu\text{m}$  at the highest volume fraction  $F \approx 10^{-3}$
- Reasonable agreement with expected  $l_{NP} = \frac{4r}{3F}$



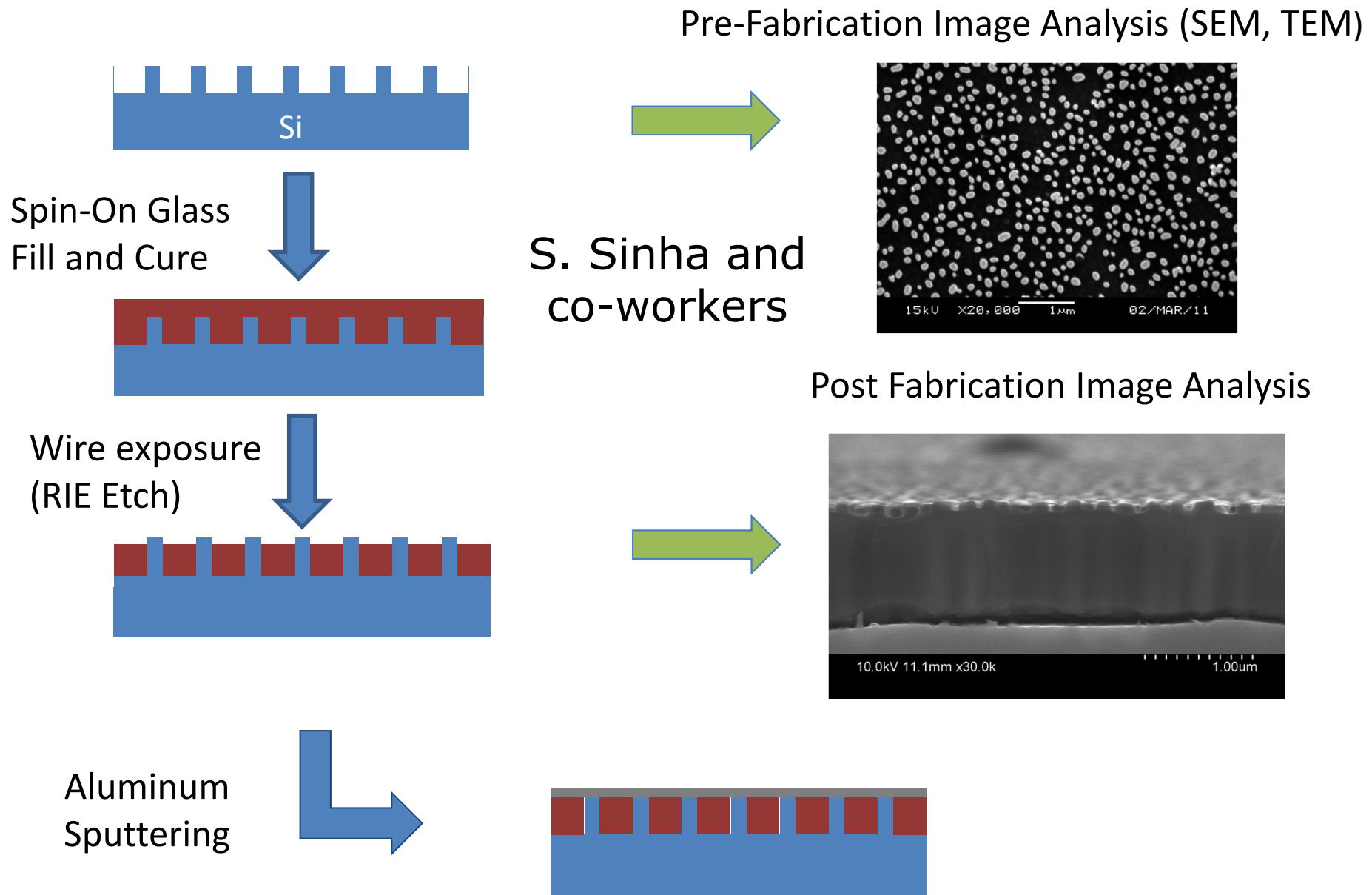
Worlock, PR 147, 636 (1966)

# New phonon physics in roughened nanowires?

Single Si nanowire measurements by Majumdar, Yang, and co-workers (2008)

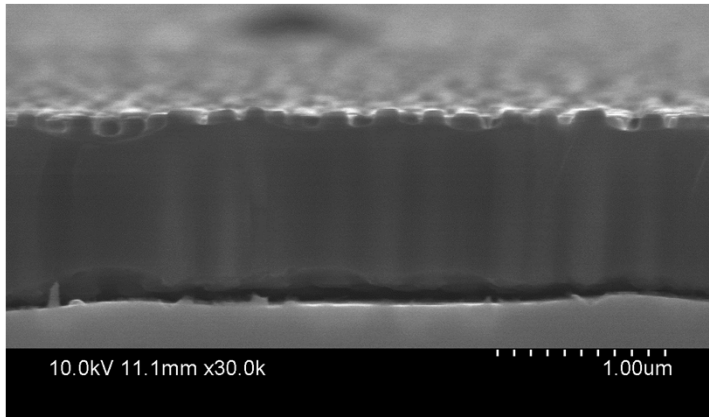


# Sample Process Flow for Si nanowire arrays

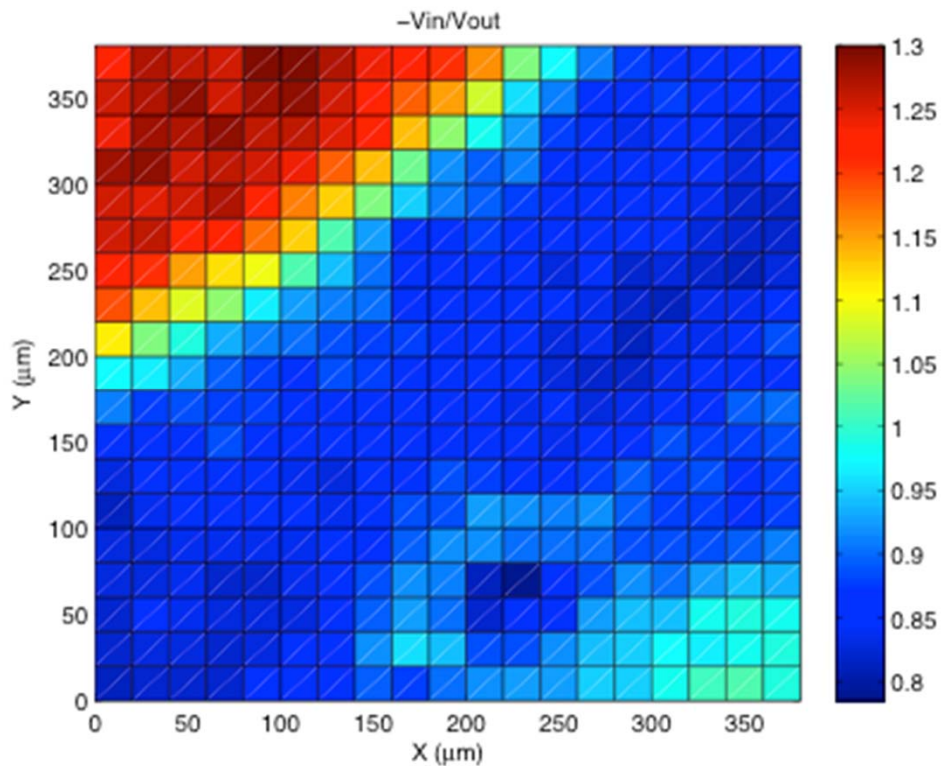
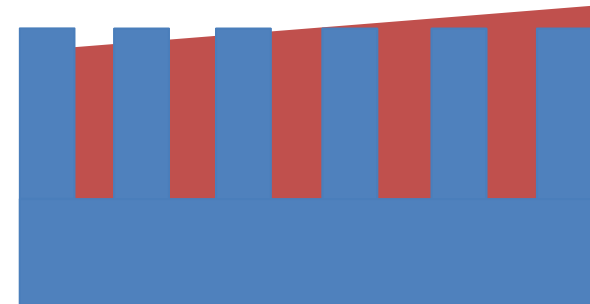




# ● Make use of high spatial resolution of TDTDR



Penetration Depth at 10 MHz  
in Spin-On Glass: ~50nm

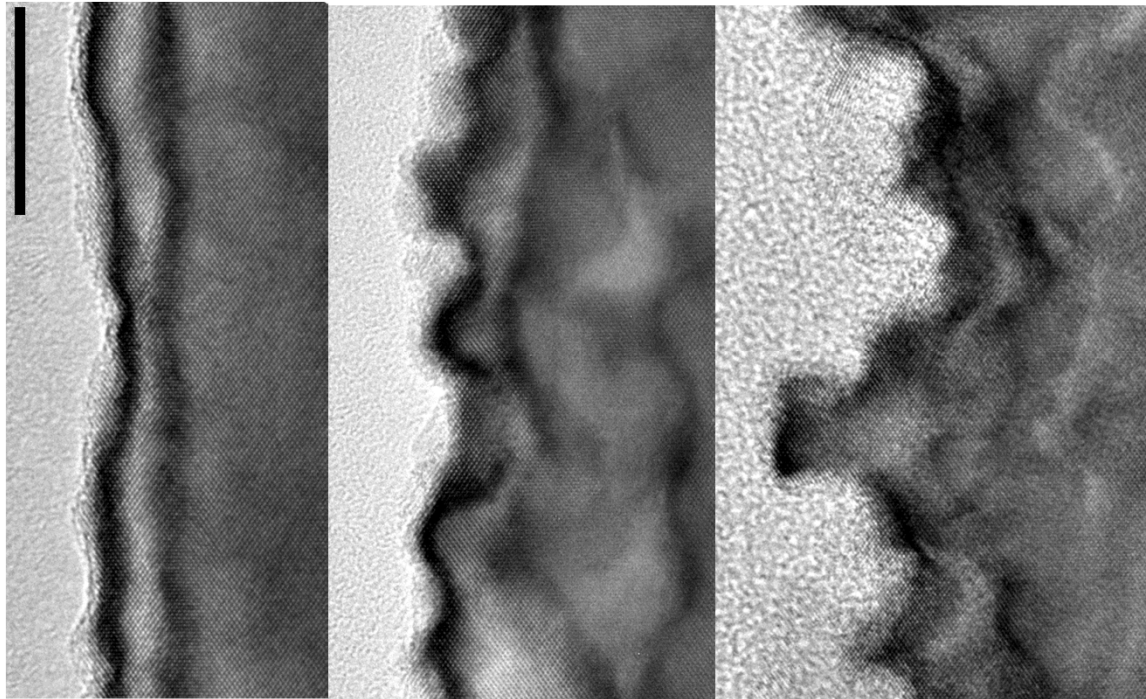


All measurements are taken  
beyond the transition to the  
higher thermal conductivity  
regions

# $\approx 100$ nm diameter Si nanowires by metal-assisted etching, Au and HF/H<sub>2</sub>O<sub>2</sub>

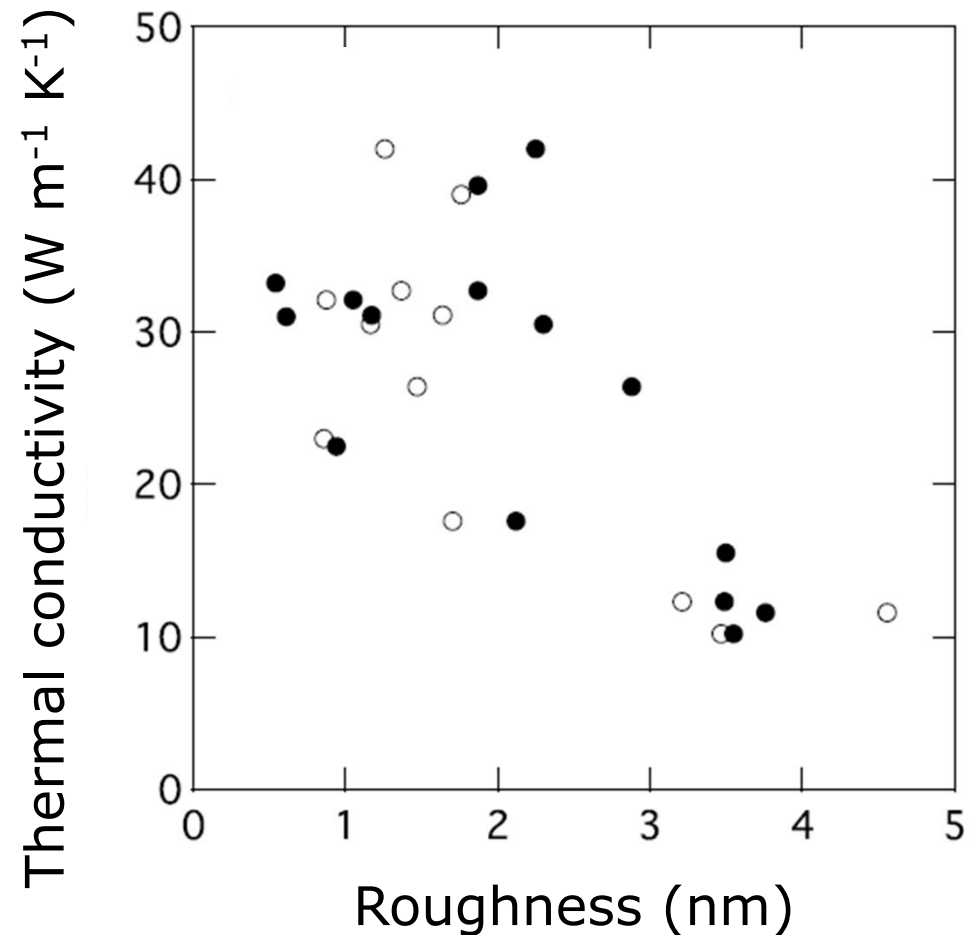
- Post-fabrication roughening using Au sputtered onto sidewalls and wet-chemistry
- Characterize roughness by TEM

↑  
10 nm  
↓



# $\approx 100$ nm diameter Si nanowires by metal-assisted etching, Au and HF/H<sub>2</sub>O<sub>2</sub>

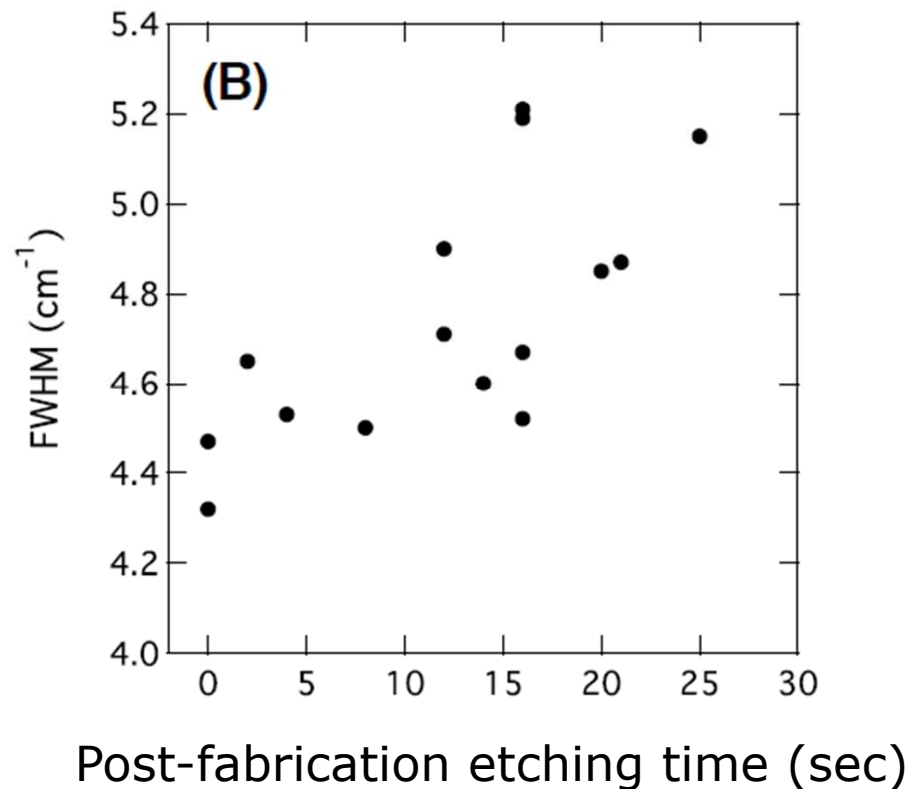
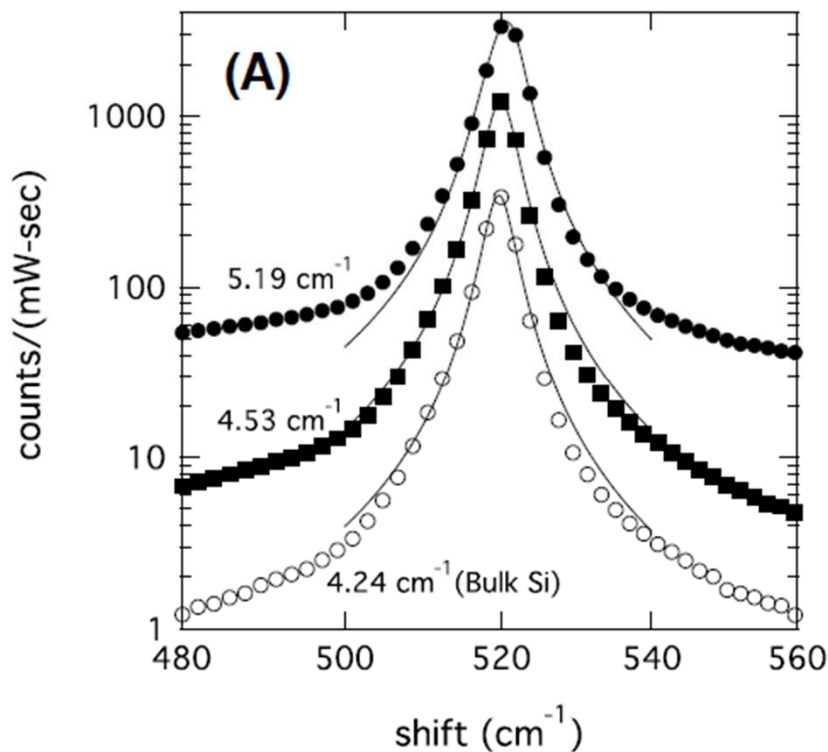
- The \$64k question: are we witnessing new physics or do the etched harbor defects that are not apparent by TEM.
- TEM is typically great for extended defects but not that sensitive to point defects or clusters of point defects.



Feser *et al.*, submitted

# Raman peak broadens with etching time

- Consequence of roughness (e.g., inhomogeneous strain fields, confinement) or does etching inject defects?



Feser *et al.*, submitted

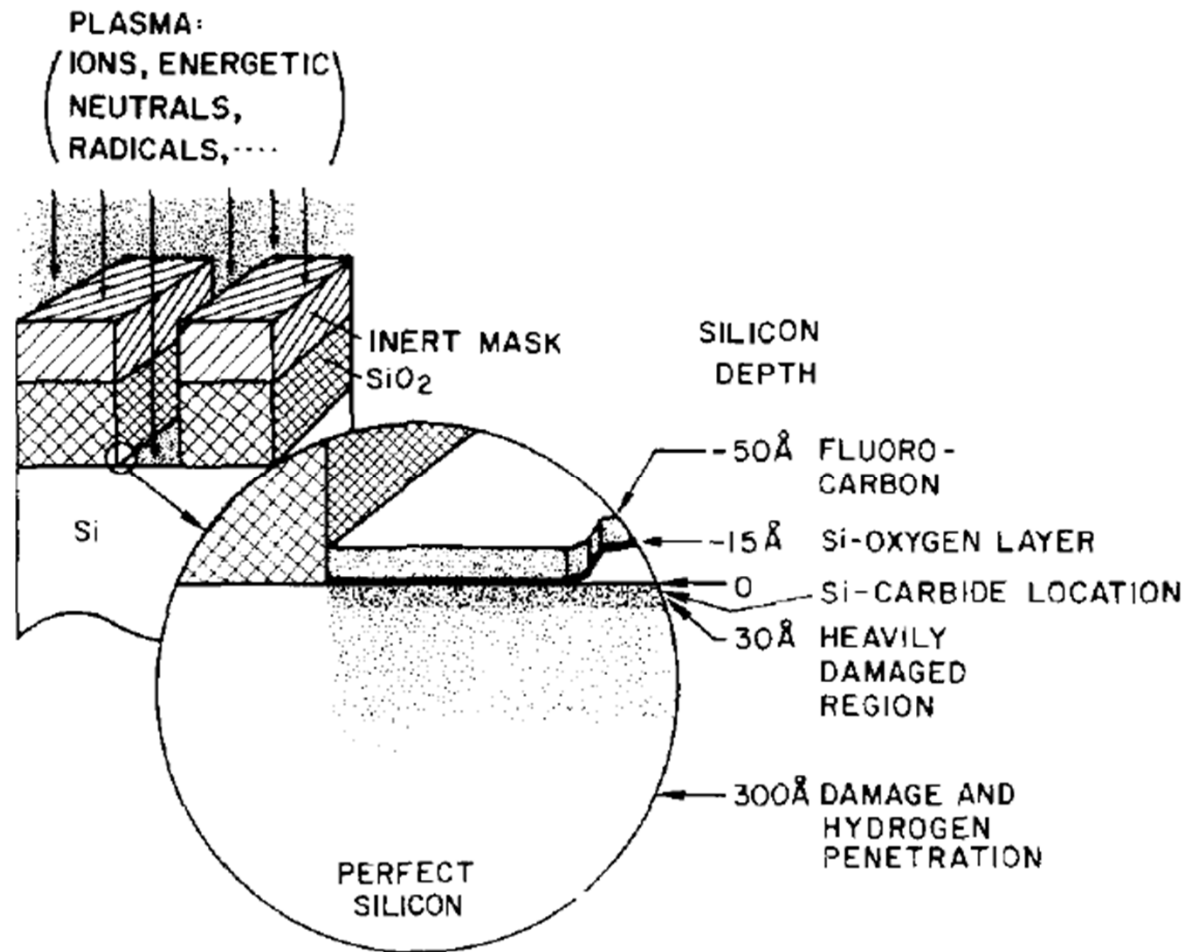
# Defects happen...

- Not the same, of course, but extensive damage from dry etching of Si was not expected either

## Dry Etching Damage of Silicon: A Review

GOTTLIEB S. OEHRLEIN

*IBM Research Division, Thomas J. Watson Re:*



# Conclusions

- Superlattice interfaces can be used to reduce thermal conductivity but lowest conductivity is typically above the amorphous limit. Even the best superlattice interfaces are diffuse to most thermal phonons at room temperature.
- PbSe nanodots are not very effective in lowering the thermal conductivity of PbTe. Essentially the same thermal conductivity is observed in alloys with the same average composition. This can be understood based on strong anharmonicity and short intrinsic phonon mean-free-paths in of PbTe.
- Jury is still out on the question of new physics in rough nanowires. But we can conclude that the low thermal conductivities observed in single nanowire measurements are not easy to reproduce. Does metal-assisted etching create damage, e.g., vacancy/hydrogen complexes or clusters?