

# Thermal conductance of solid-liquid interfaces

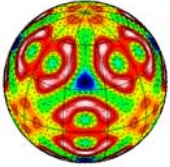
Scott Huxtable, Zhenbin Ge, David G. Cahill  
*Frederick Seitz Materials Research Laboratory*  
*Department of Materials Science*  
*University of Illinois, Urbana*

Sergei Shenogin, Harshit Patel, Pawel Keblinski  
*Materials Science and Engineering Department*  
*Rensselaer Polytechnic Institute*



**Rensselaer**

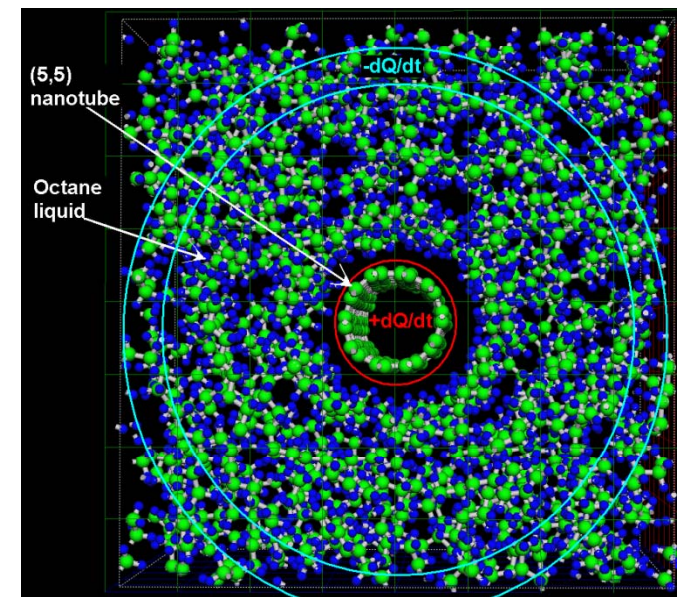
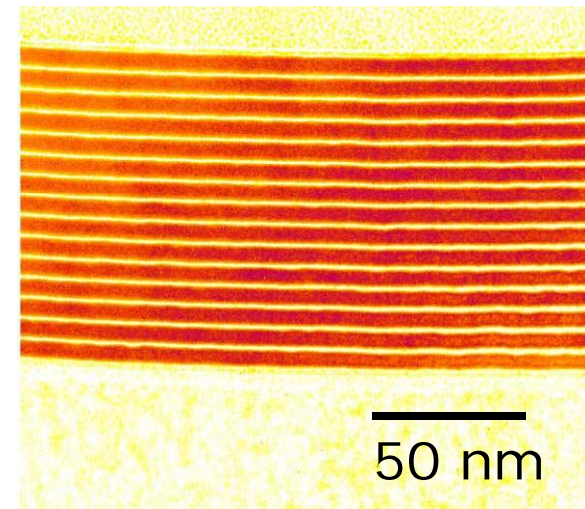


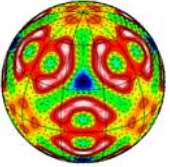


# Interfaces are critical at the nanoscale



- Low thermal conductivity in nanostructured materials
  - improved thermoelectric energy conversion
  - improved thermal barriers
- High thermal conductivity composites and suspensions
- Localization of thermal effects: medical therapy/biotechnology

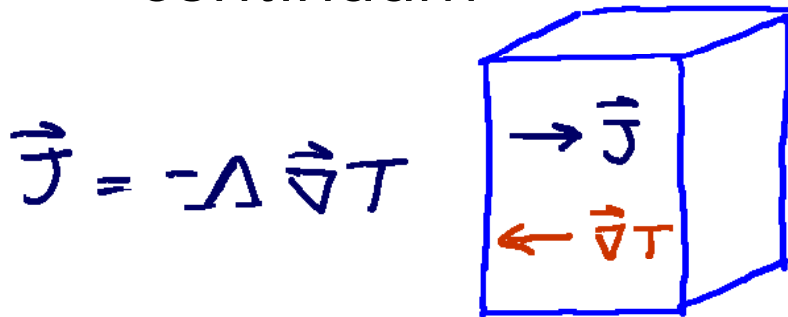




# Interface thermal conductance

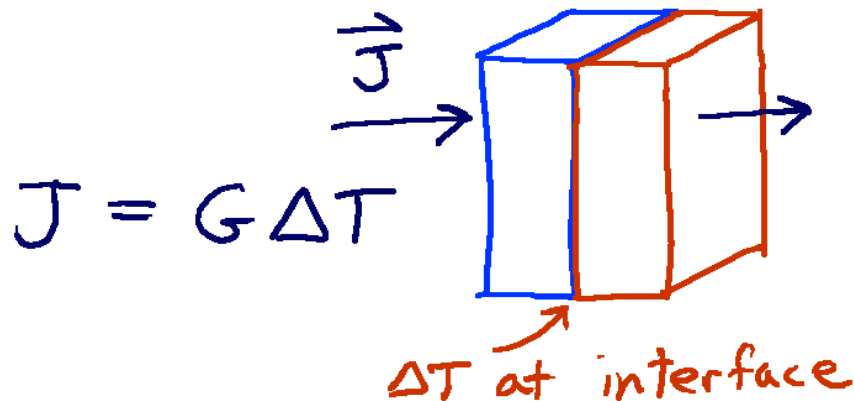


- Thermal conductivity  $\Lambda$  is a property of the continuum

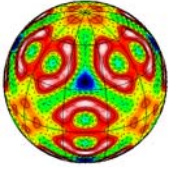


$$\Lambda = \frac{1}{3Vk_B T^2} \int_0^\infty \langle \vec{j}(t) \cdot \vec{j}(0) \rangle dt$$

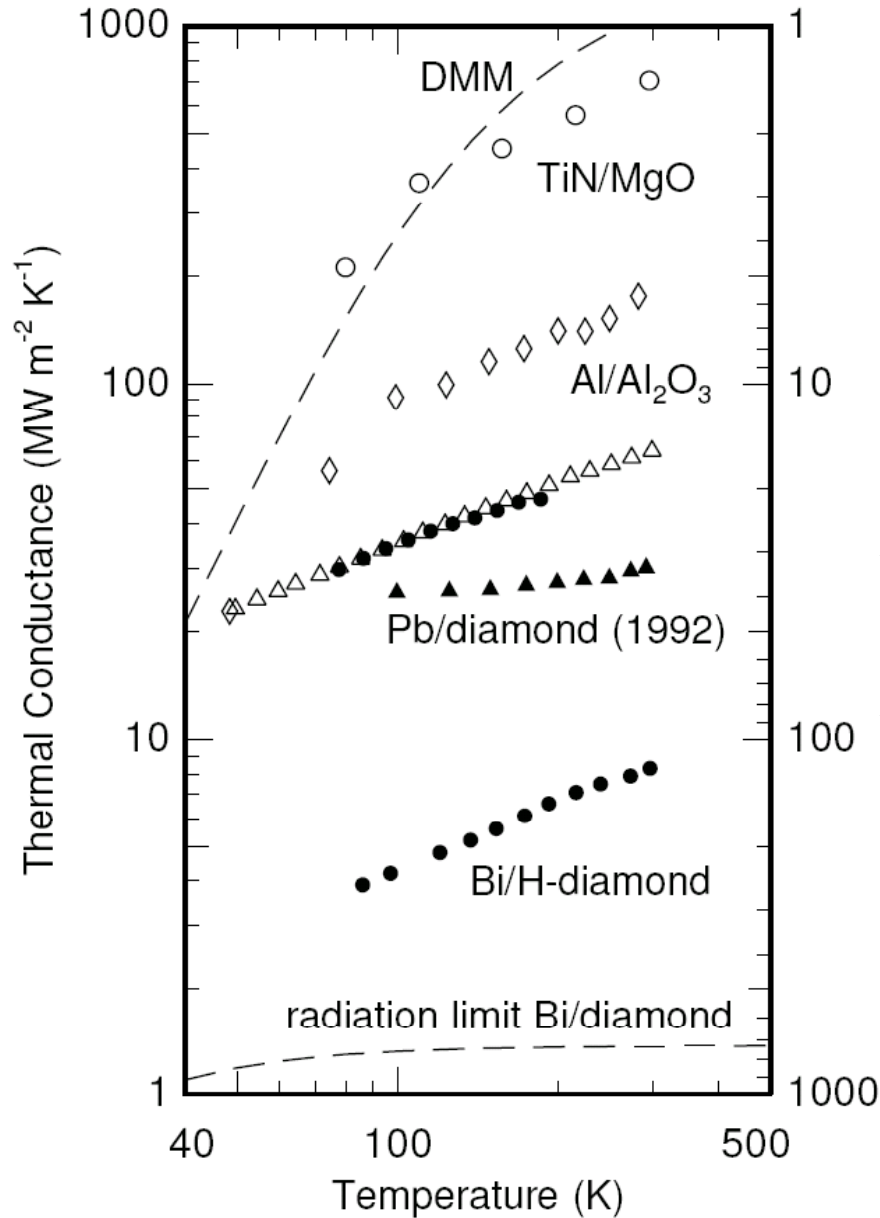
- Thermal conductance (per unit area)  $G$  is a property of an interface



$$G = \frac{1}{Ak_B T^2} \int_0^\infty \langle q(t)q(0) \rangle dt$$



# Factor of 60 range at room temperature

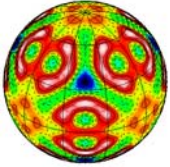


← Au/surfactant/water

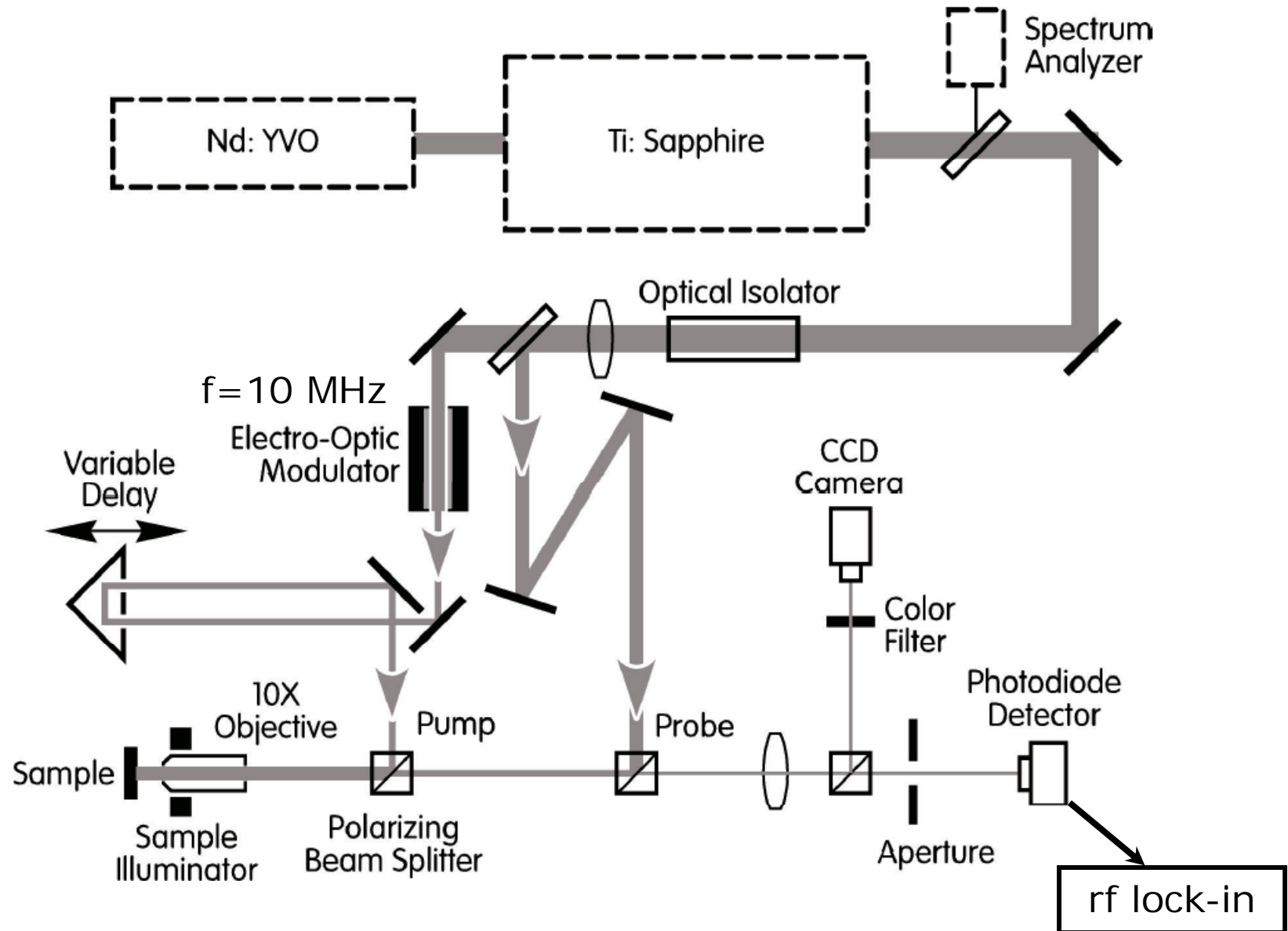
← PMMA/ $\text{Al}_2\text{O}_3$

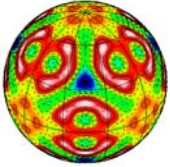
← nanotube/alkane

Equivalent Film Thickness (nm)



# Modulated pump-probe apparatus

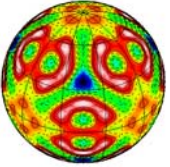




## Solid-liquid interfaces: Two approaches



- Transient optical absorption of nanoparticles and nanotubes in liquid suspensions.
  - Measure the thermal relaxation time of a suddenly heated particle. Interface sensitive if the particle is small enough.
  - limited to interfaces that give good stability of the suspension, e.g., hydrophilic particles in H<sub>2</sub>O
- Time-domain thermoreflectance of thin planar Al and Au films.
  - heat flows both directions: into the fluid and into the solid substrate.

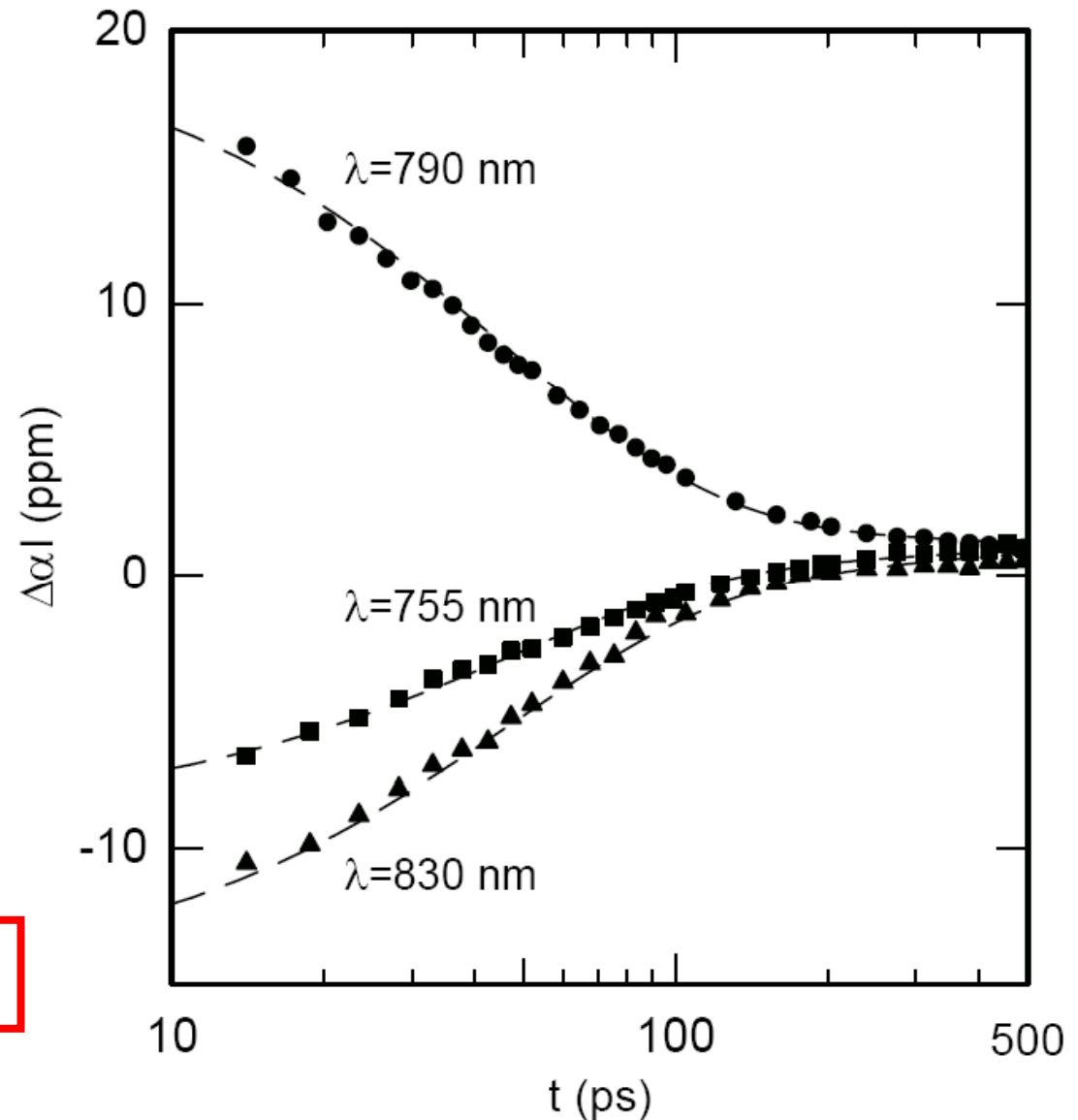


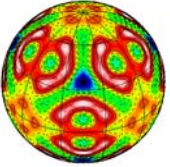
# Nanotubes in surfactant in water: Transient absorption



- Optical absorption depends on temperature of the nanotube
- Assume heat capacity is comparable to graphite
- Cooling rate (RC time constant) gives interface conductance

$$G = 12 \text{ MW m}^{-2} \text{ K}^{-1}$$





## Application: Critical aspect ratio for a fiber composite



- Isotropic fiber composite with high conductivity fibers (and infinite interface conductance)

$$\Lambda_c = \frac{1}{3} V_f \Lambda_{NT}$$

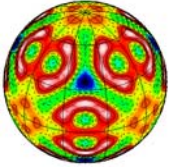
- But this conductivity is obtained only if the aspect ratio of the fiber is high

$$3 \left( \frac{\Lambda_{NT}}{rG} \right)^{1/2} \approx 2000$$

- Troubling question: Did we measure the relevant value of the conductance?

"heat capacity G" vs. "heat conduction G"





# Comparisons between experiment and simulation: general considerations

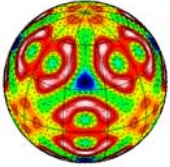


## Experiment

- optical pulse creates electronic excitations which decay
  - electron-phonon
  - phonon-phonon
- high frequency vibrations are quantized
- interfaces are difficult to prepare and characterize

## Simulation

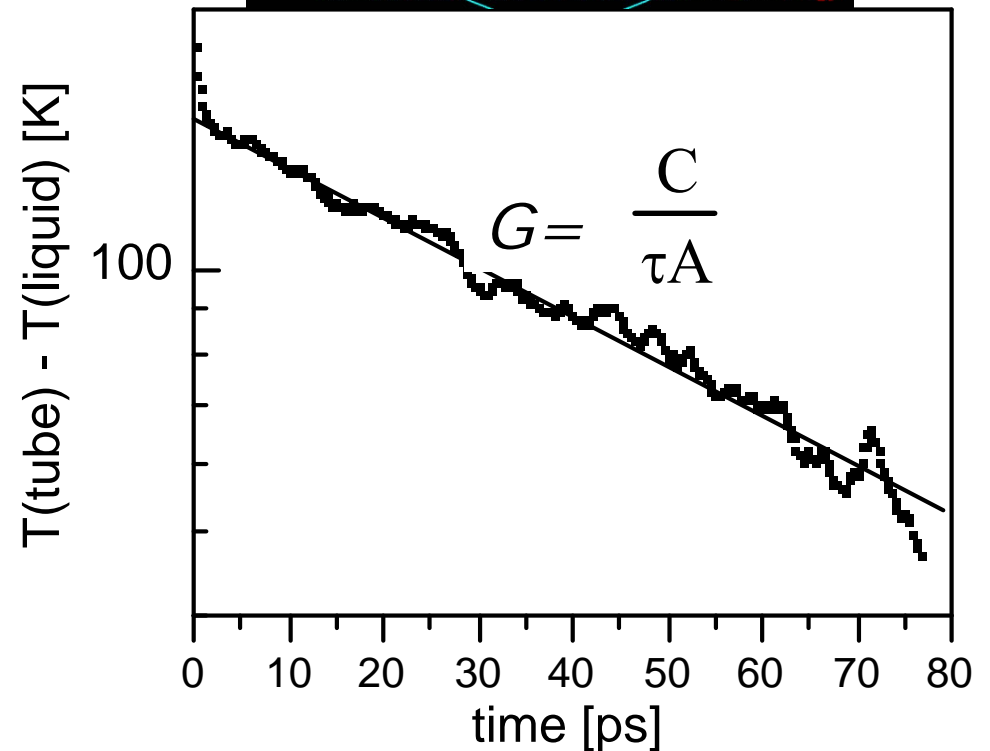
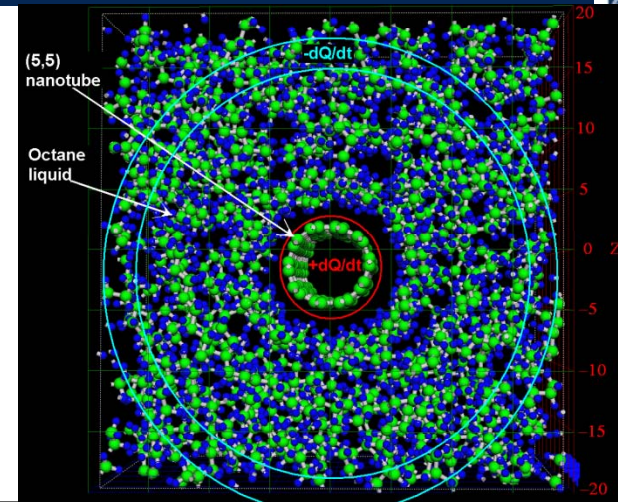
- no electrons but can add heat any way we want
- all vibrational modes are thermally excited.
- uncertainties in potentials
- finite-size simulation cell removes lowest-frequency vibrations and creates problems for long mean-free-paths

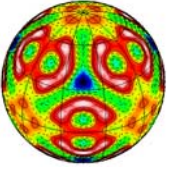


# Simulation: relaxation time

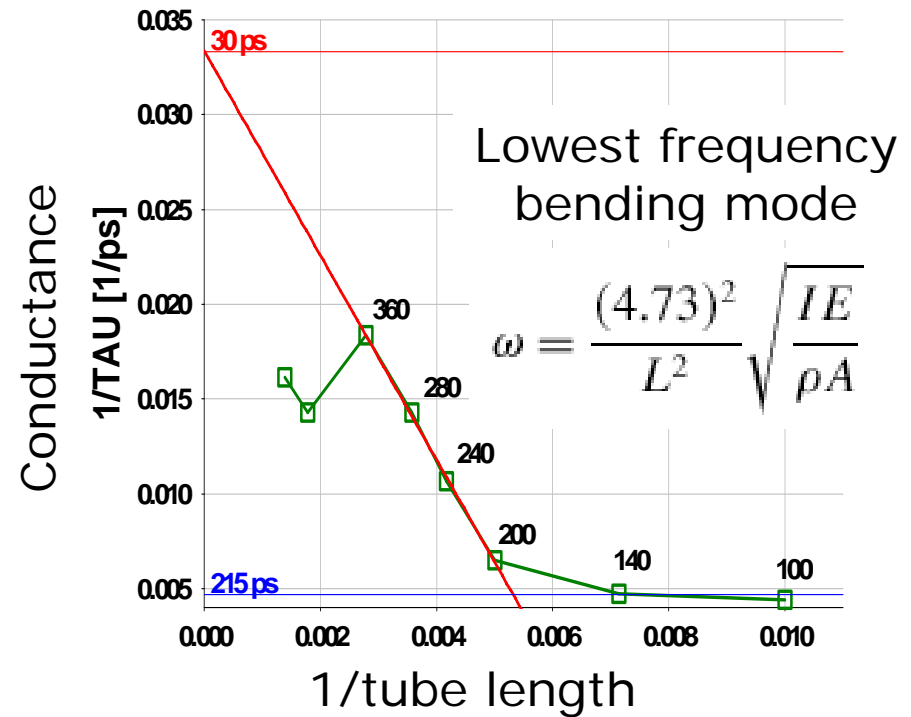
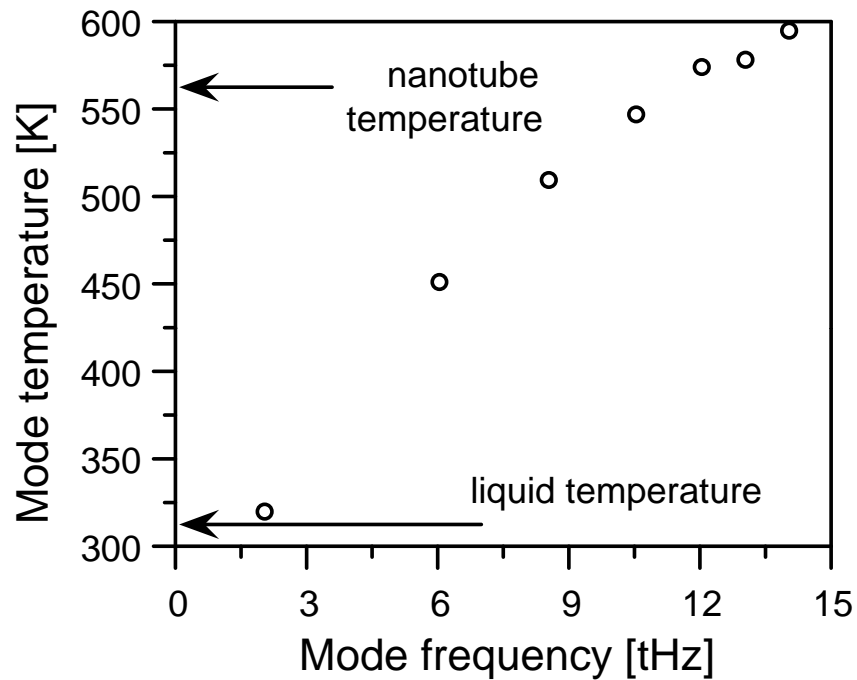


- Mimic the experiment: heat nanotube suddenly and let system equilibrate
- Use experimental heat capacity to convert time constant to  $G$ . For long tubes:  
$$G = 22 \text{ MW m}^{-2} \text{ K}^{-1}$$

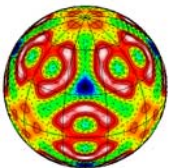




# Simulation: Mechanisms for interface heat conduction



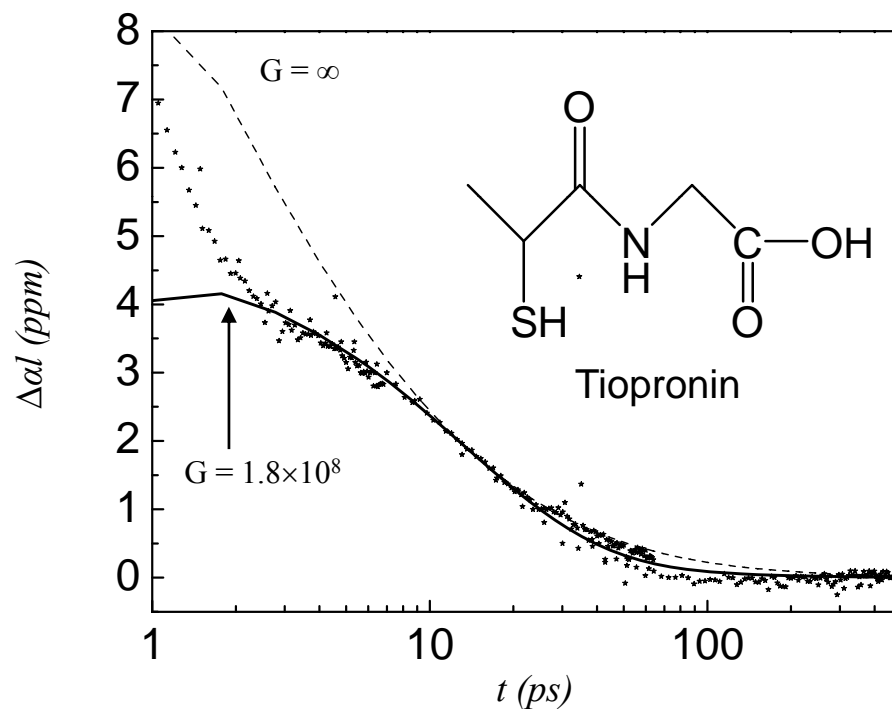
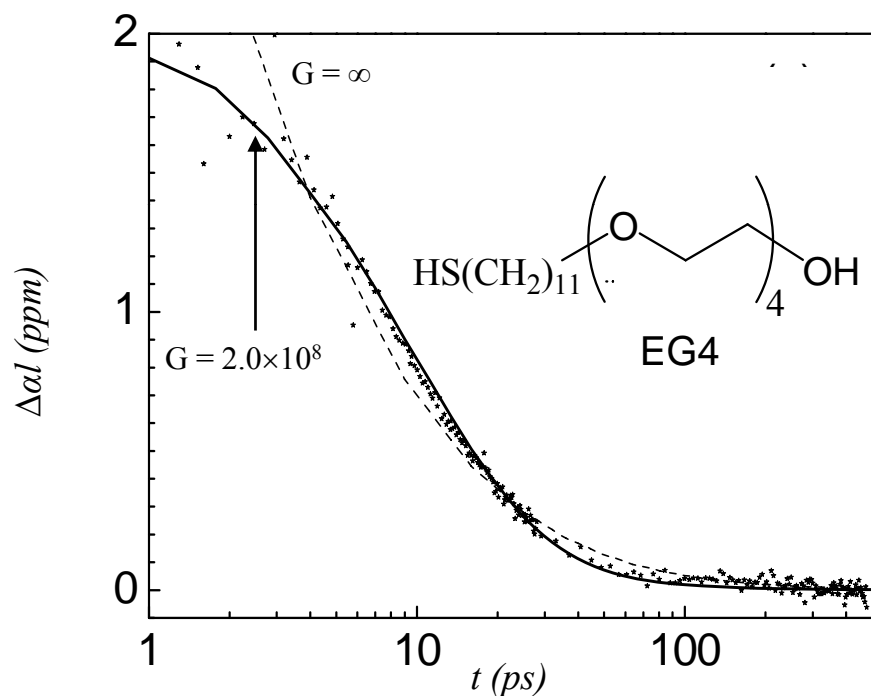
- Carbon nanotubes have a small number of low frequency modes associated with bending and squeezing. Only these modes can couple strongly with the liquid.

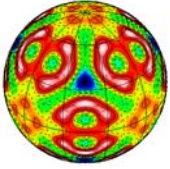


# Hydrophilic metal nanoparticles: 4 nm diameter Au:Pd nanoparticles in water



- transient absorption data



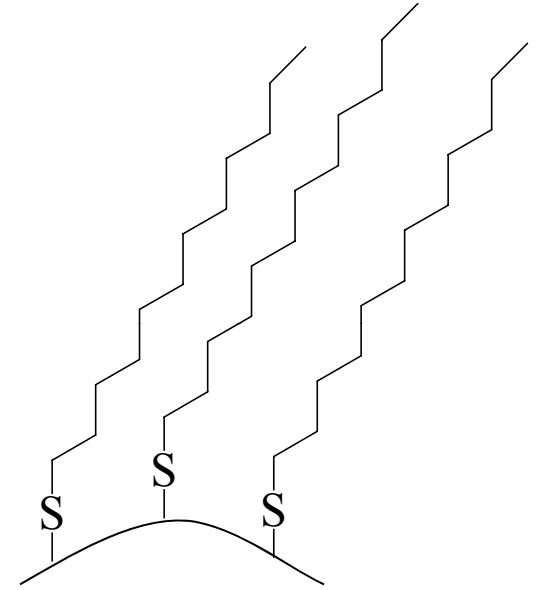
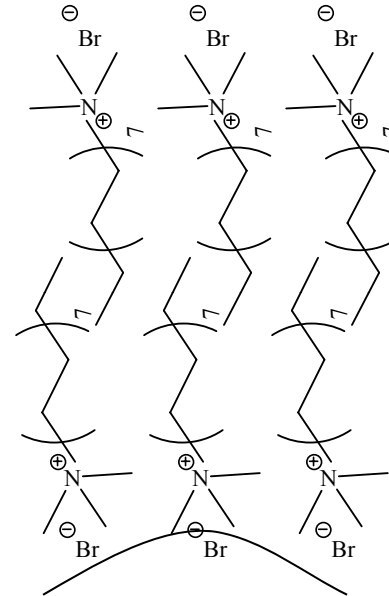
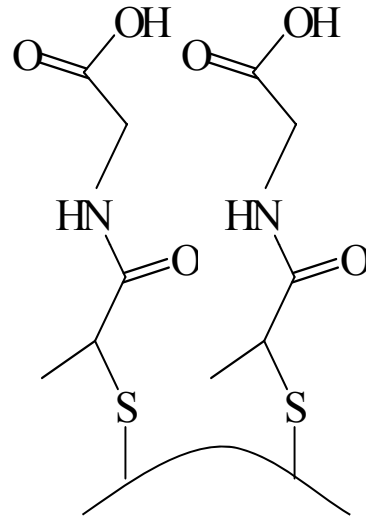
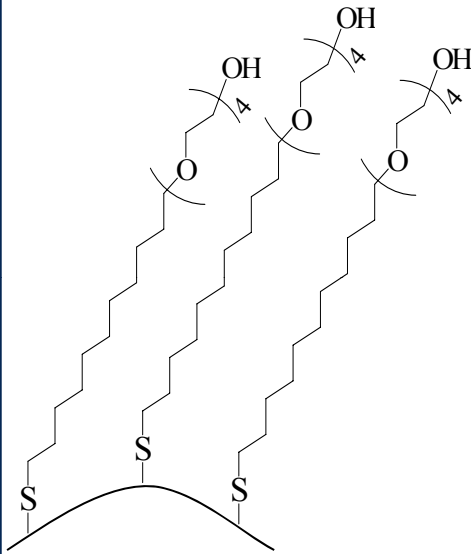


# Nanoparticle summary



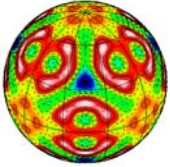
In water

In Toluene



$G \sim 200 \text{ MW m}^{-2} \text{ K}^{-1}$

$G \sim 15 \text{ MW m}^{-2} \text{ K}^{-1}$



## Application: Critical particle radius for a nanofluid



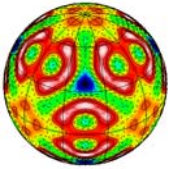
- Interface conductance and thermal conductivity of the fluid determine a critical particle radius

$$r_c = \Lambda/G$$

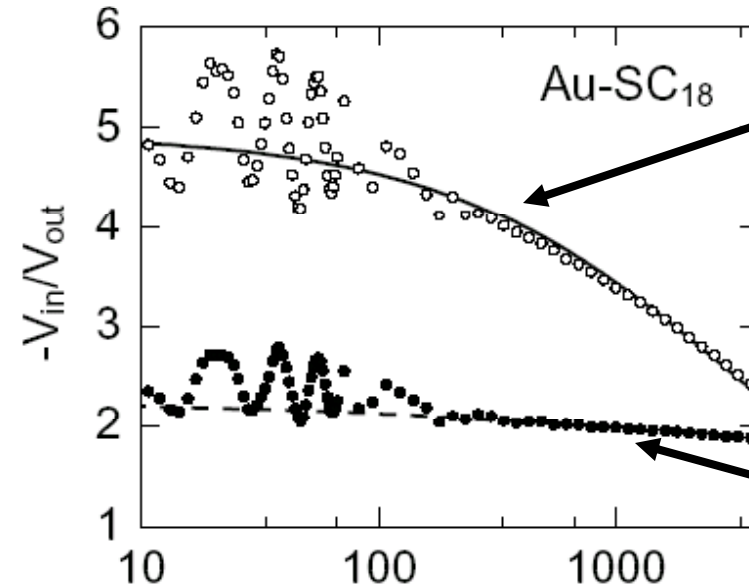
- For particles in water,  $r_c = 3$  nm.
- For high thermal conductivity particles, dilute limit of effective medium theory

$$r \gg r_c \quad \Delta\Lambda = (1+3\phi)\Lambda$$

$$r \ll r_c \quad \Delta\Lambda = (1-1.5\phi)\Lambda$$

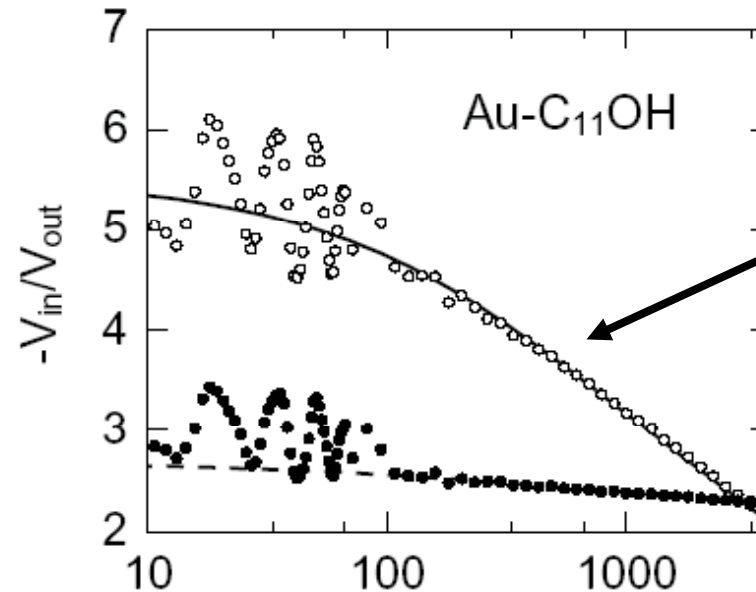


# Thermoreflectance of solid/H<sub>2</sub>O interfaces

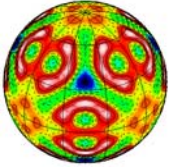


hydrophobic  
50 MW/m<sup>2</sup>-K

no water



hydrophilic  
100 MW/m<sup>2</sup>-K

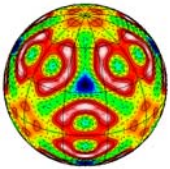


## Thermoreflectance of solid/H<sub>2</sub>O interfaces

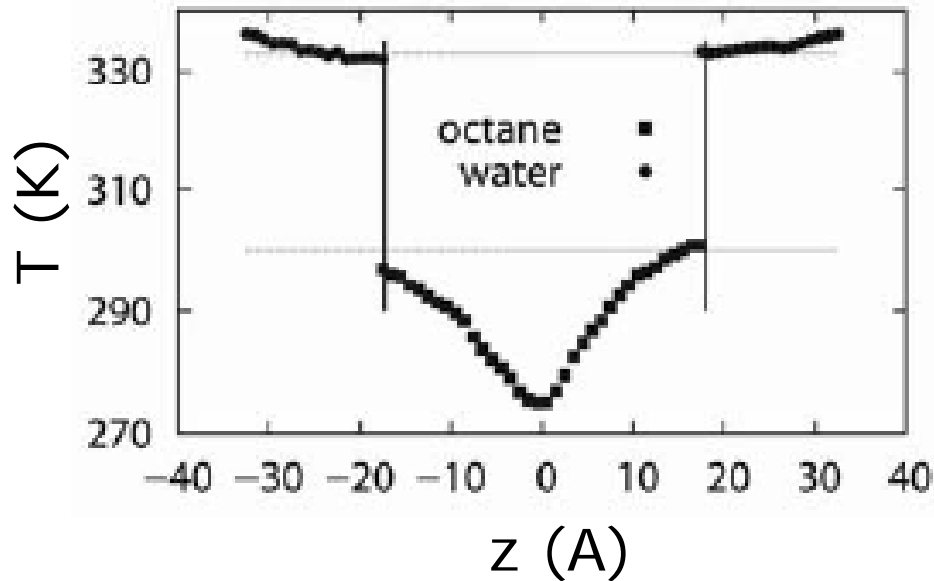
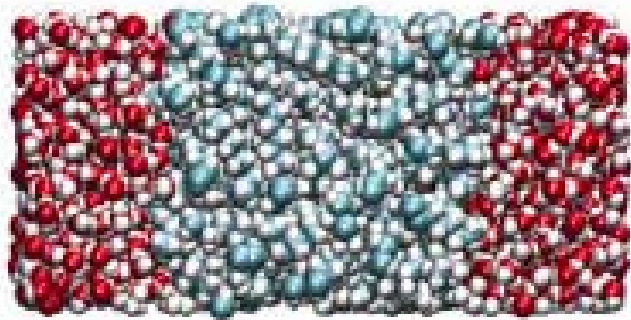


- Experiments contain many interfaces and layers so look at the difference in the conductance created by changing from hydrophobic to hydrophilic.
- Define Kapitza length, equivalent thickness of water:  $h = \Lambda/G$ 
  - Au/hydrophobic  $h = 12$  nm
  - Au/hydrophilic  $h = 6$  nm
- Difference  $\Delta h = 6$  nm

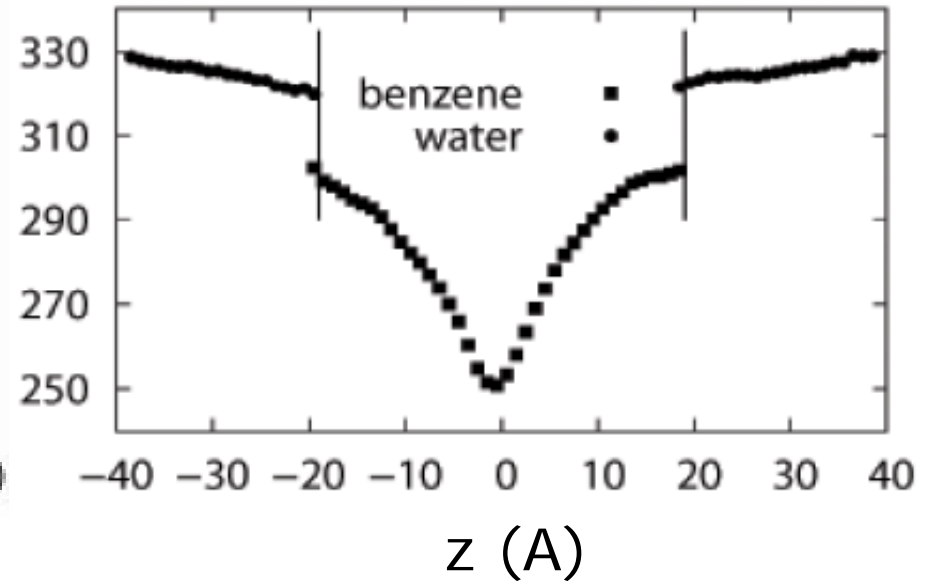




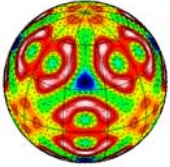
# Simulation of model interfaces



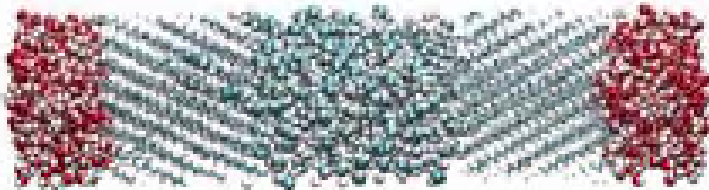
water-octane  
 $G = 65 \text{ MW/m}^2\text{-K}$



water-benzene  
 $G = 175 \text{ MW/m}^2\text{-K}$

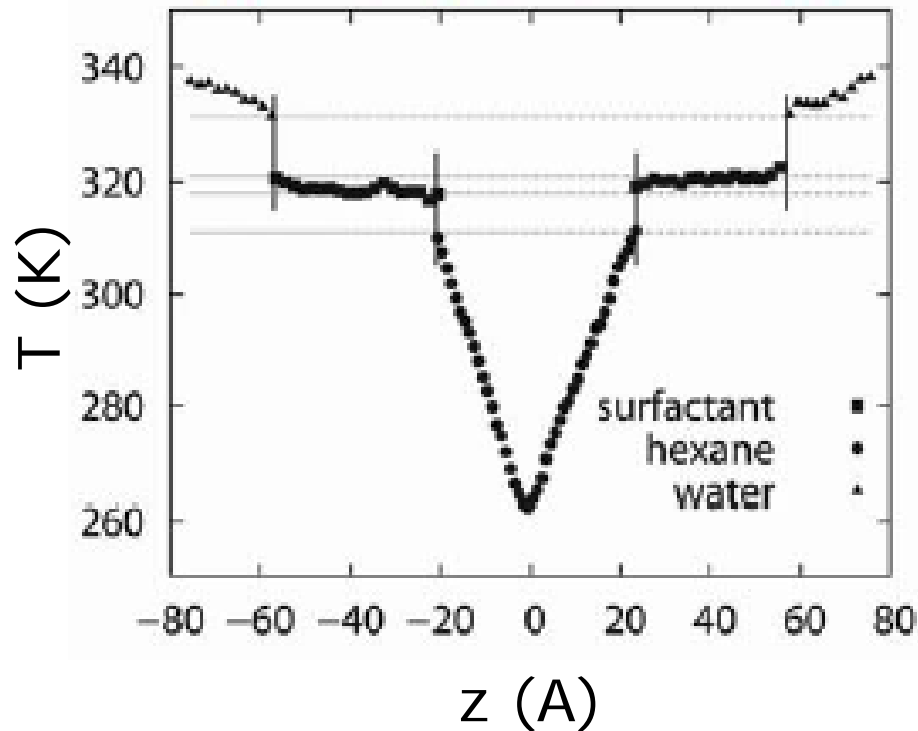


# Water - Surfactant - Hexane Interface



$$G_{\text{H}_2\text{O-surf}} = 300 \pm 30 \text{ MW/m}^2\text{-K}$$

$$G_{\text{surf-hex}} = 370 \pm 30 \text{ MW/m}^2\text{-K}$$

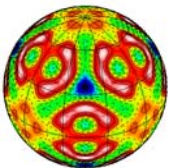


High conductivity of the ordered surfactant

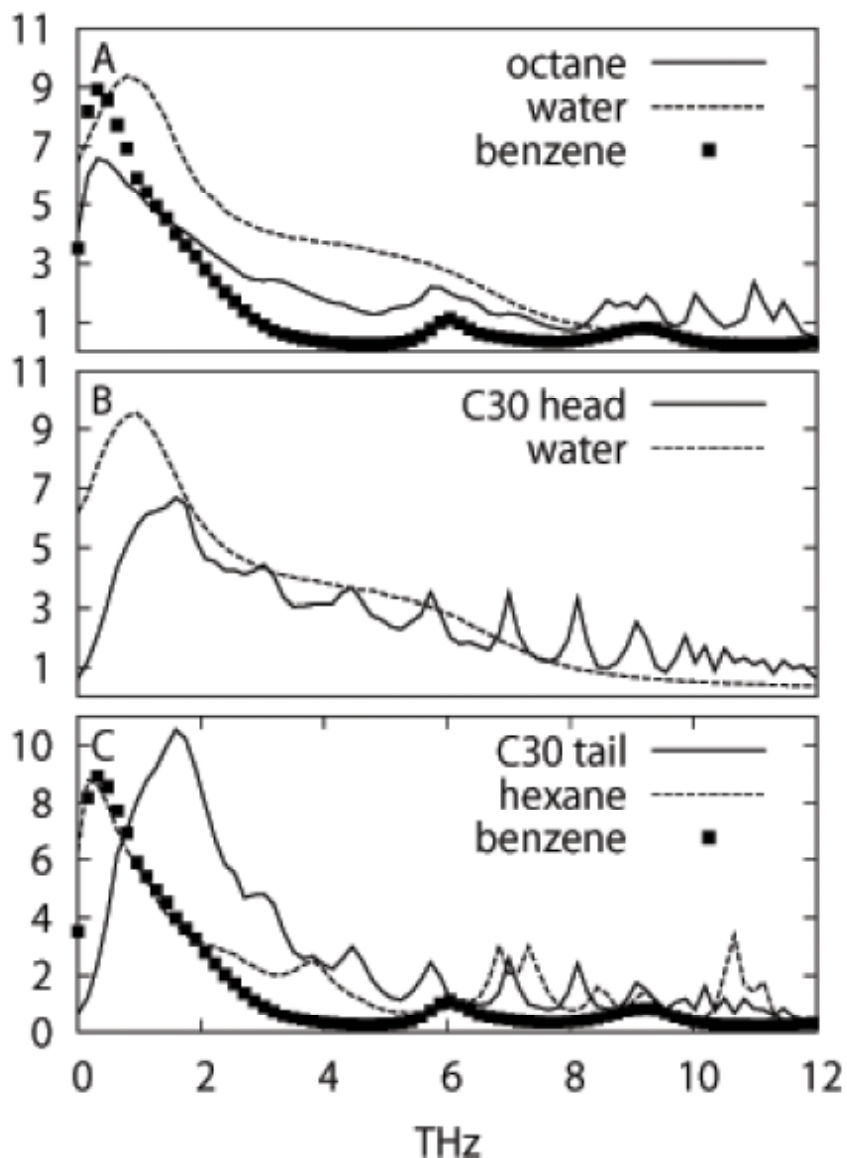
$$\Lambda_{\text{surfactant}} = 9 \text{ W/m-K}$$

$$\Lambda_{\text{hexane}} = 0.11 \text{ W/m-K}$$

(0.09 exp)



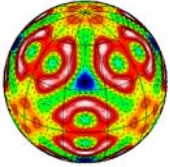
# Simulated vibrational spectra



Interface	$G$ (MW/m <sup>2</sup> -K)	$\Delta-H_2O/G$ (nm)
Water Octane	65	9
Water Benzene	175	3.4
Water Surfactant	300	2
Surfactant Hexane	370	1.6
Surfactant Benzene	190	3

difference between  
water/octane and  
water/surfactant

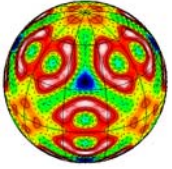
$$\Delta h = 7 \text{ nm}$$



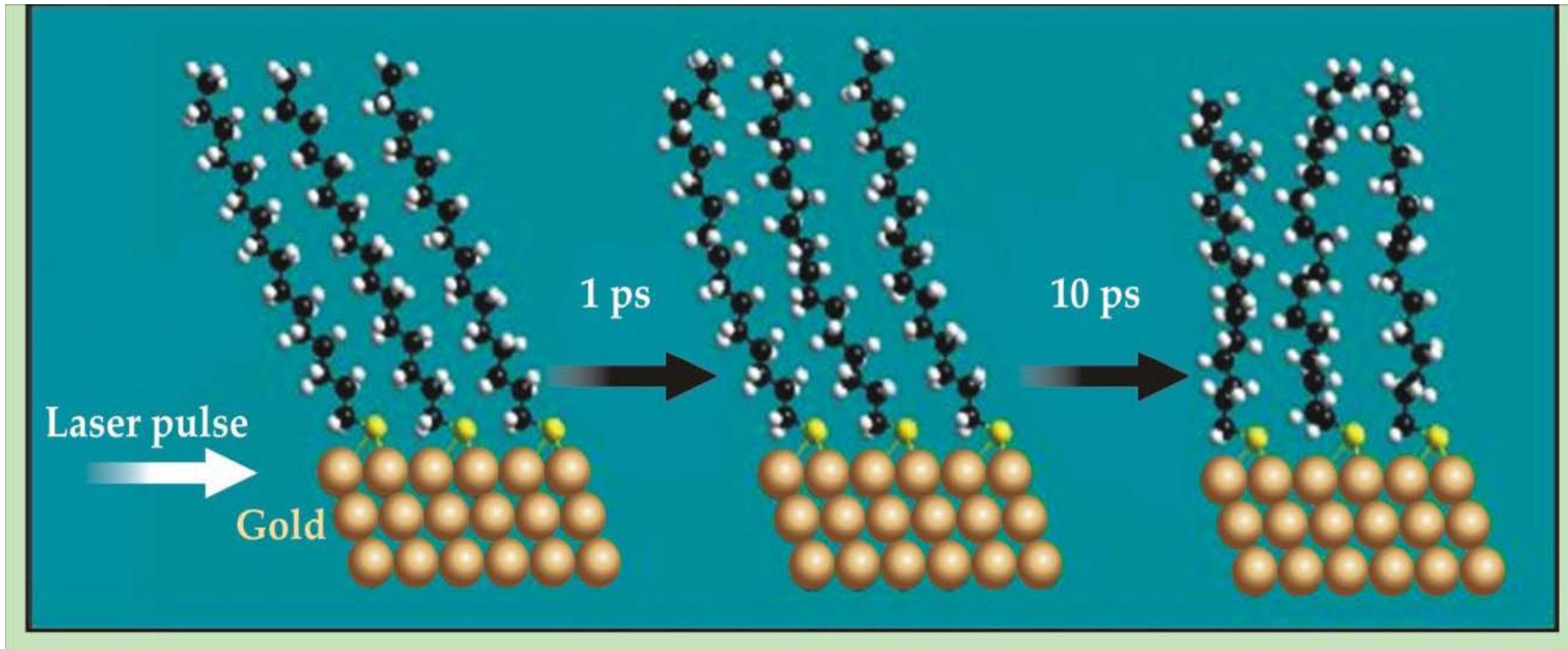
## Summary (so far)

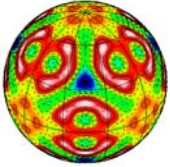


- Simulations of nanotube/octane show twice the conductance of experiment on nanotube/alkane-surfactant.
  - experiment: nanotubes form small bundles? large electron-to-phonon-to-phonon resistance?
  - simulation: lack of quantization?
  - both: surfactant structure?
- The difference in Kapitza lengths for hydrophobic and hydrophilic interfaces is nearly identical in simulation and experiment.
  - experiment 6 nm (for Au) and 7 nm (for Al)
  - simulation 7 nm
- Large discrepancy for organic-organic interfaces: need to revisit the experiments.

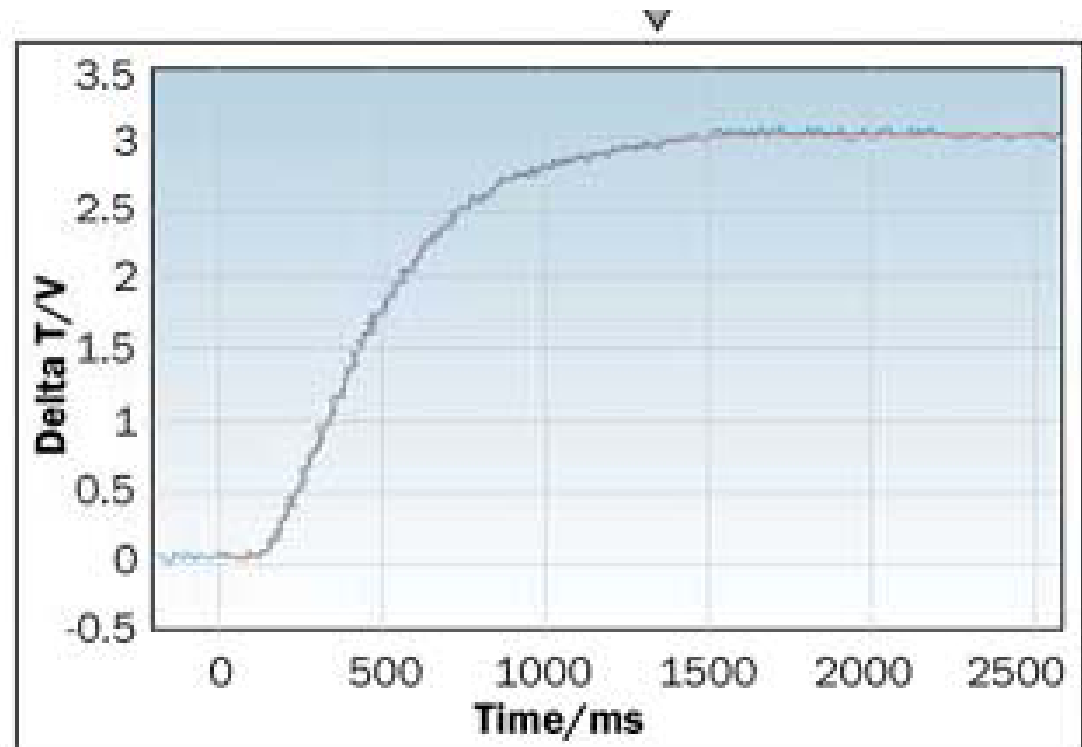
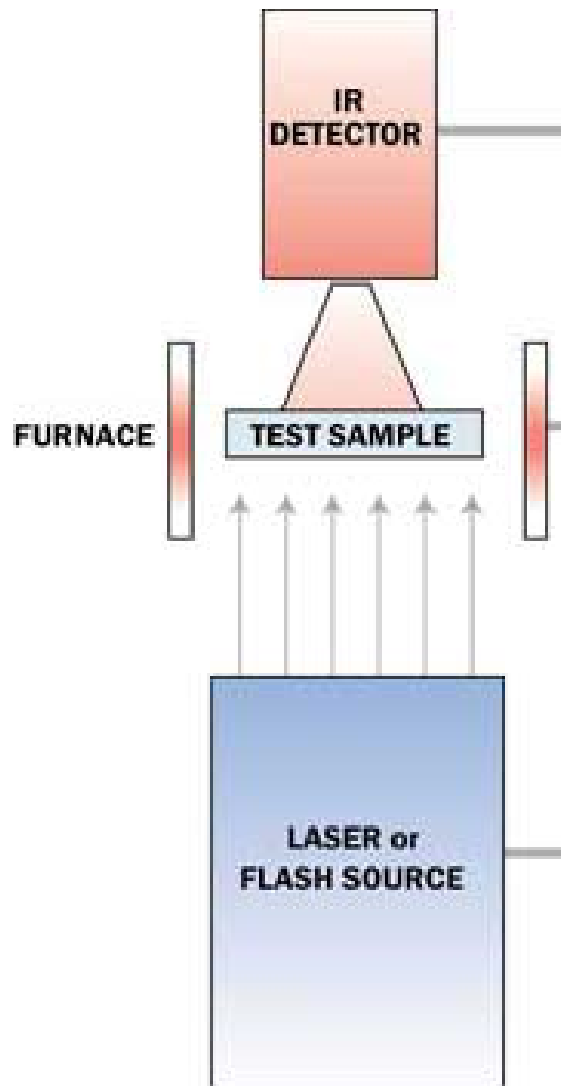


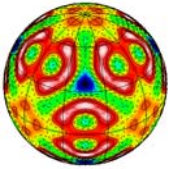
# Heat transport and ultrafast disordering of an organic molecule (with Dana Dlott)





# Classic "flash diffusivity" measurement

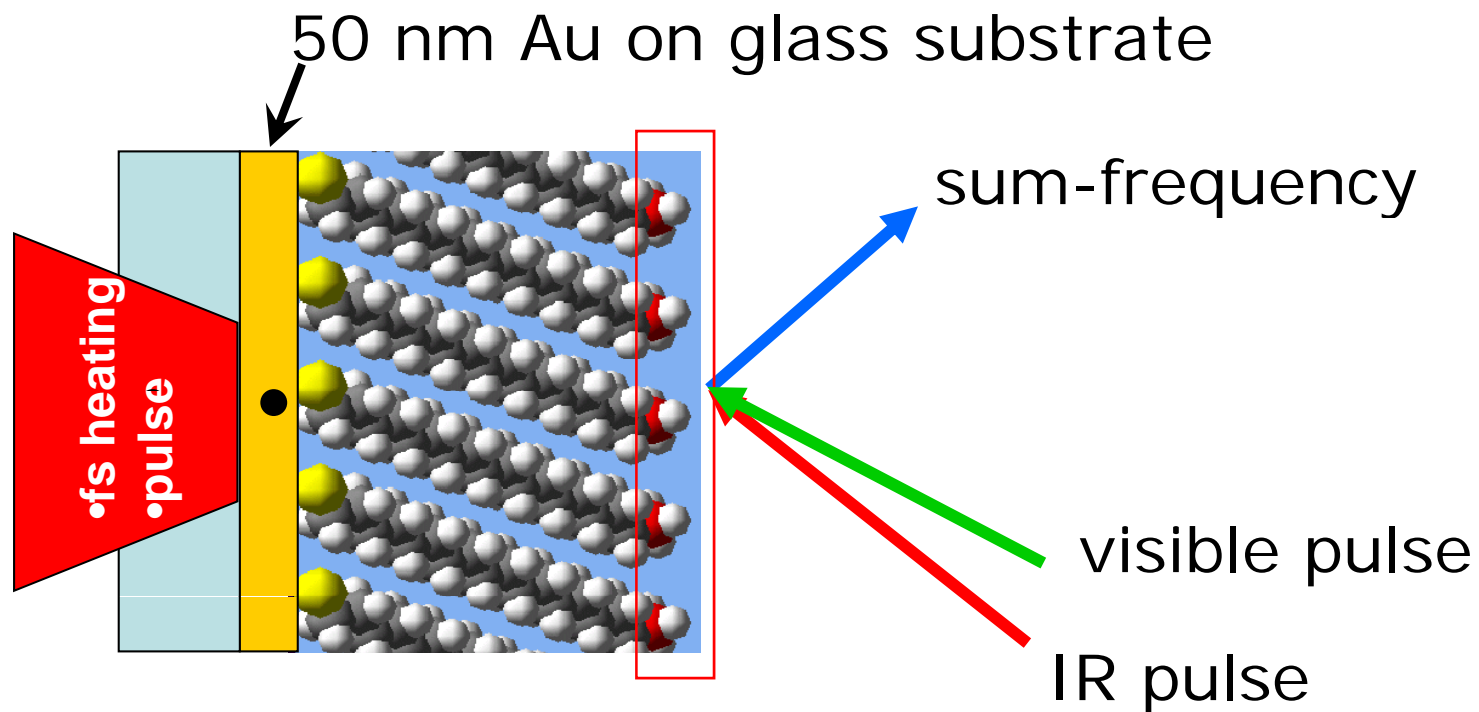


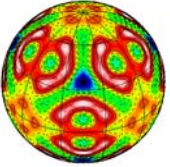


# Broad-band sum-frequency generation (SFG) vibrational spectroscopy



- tunable (2.5-18  $\mu\text{m}$ ) broad-band IR pulse
- fixed (800 nm) narrow band
- sum-frequency signal analyzed by spectrograph

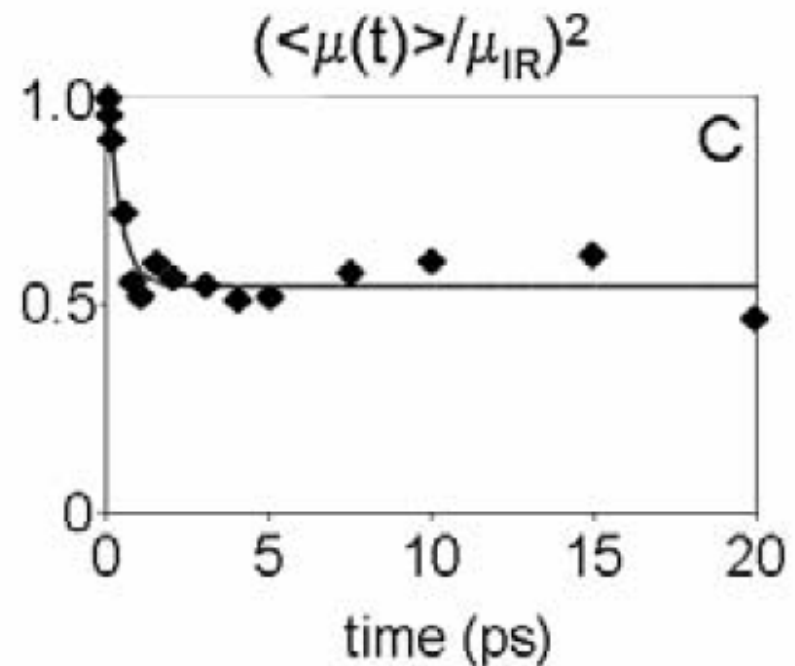
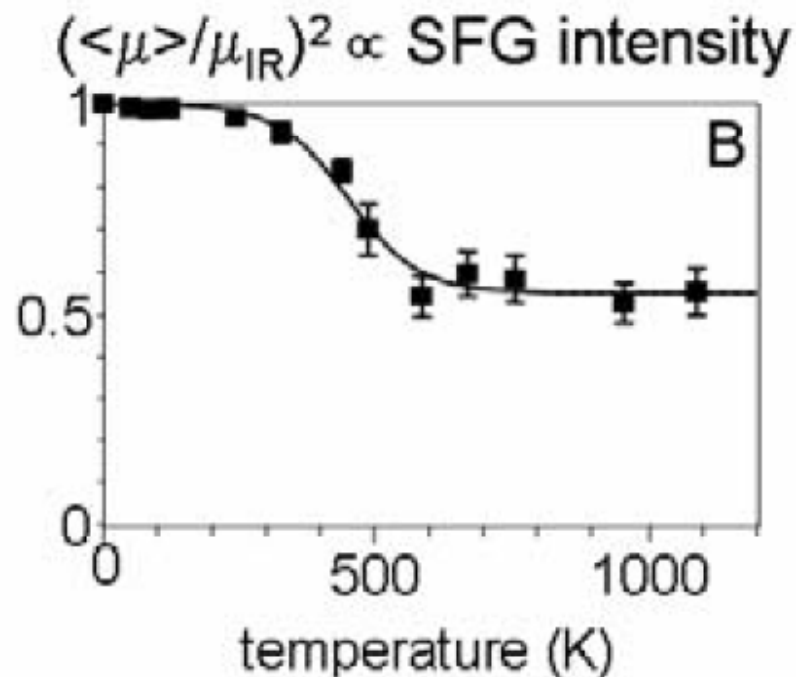




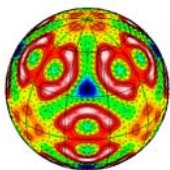
# Complicated thermometer



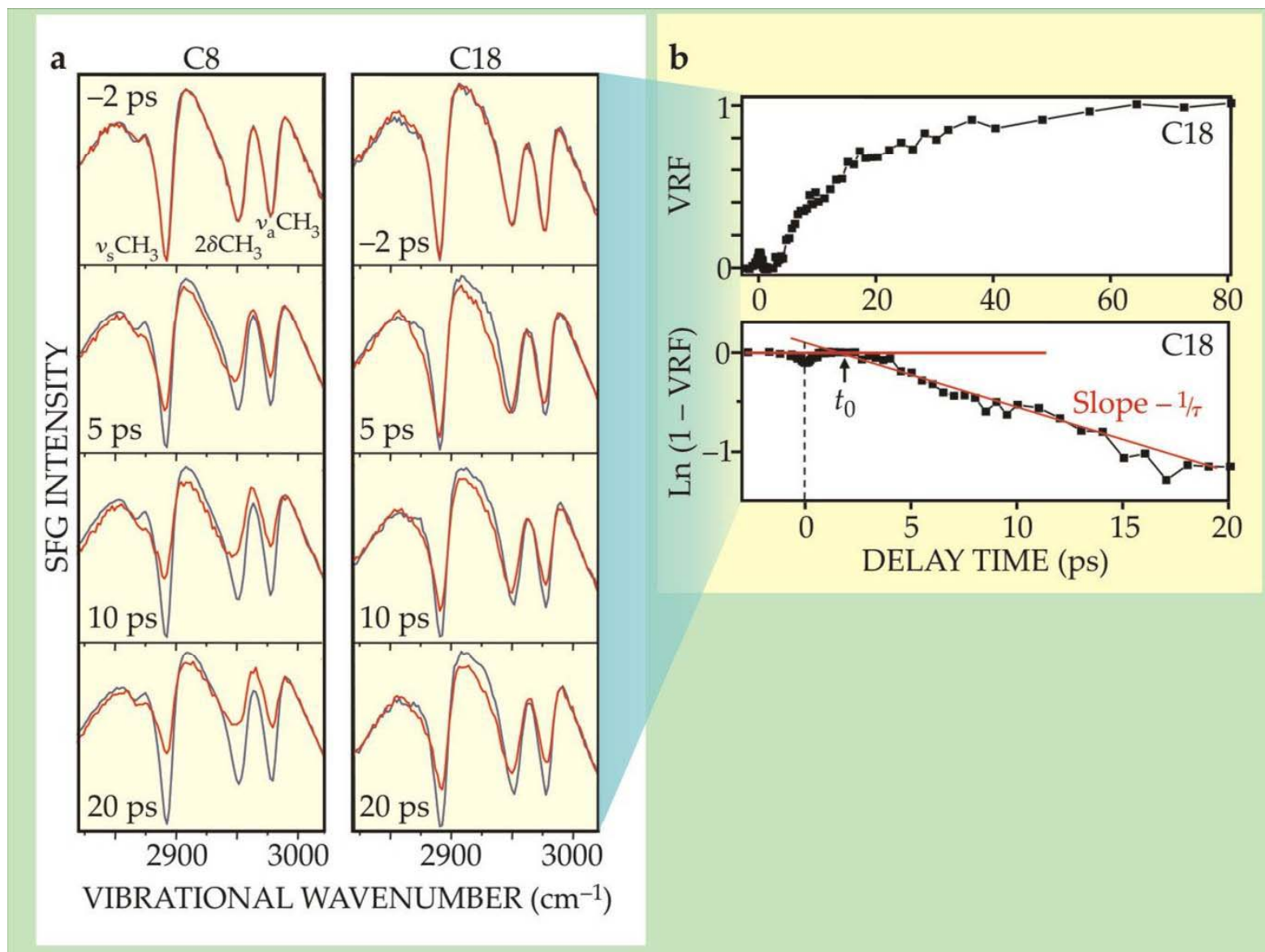
- MD simulation of suddenly heated alkane molecules: greatest sensitivity near 500 K.
- Disordering occurs in 1 ps for large (> 300 K) temperature excursion

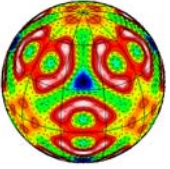






# Time-resolved sum-frequency spectroscopy





# Interface limited heat transport



- Both onset and time-constant of disordering are approximately linear in chain length
- Suggests heat transport is controlled by the interface (not diffusive in the molecule)
- Estimate of molecule heat capacity gives thermal conductance of approximately 50 pW/K

